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Nuclear Engineering
& Engineering Physics
UNIVERSITY OF WISCONSIN-MADISON

Heating and current drive – magnetically confined plasmas

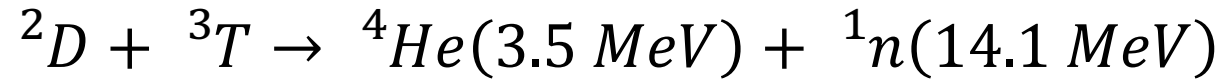
Prof. Steffi Diem, University of Wisconsin-Madison, sjdiem@wisc.edu

Summer Undergraduate Laboratory Internship Summer School

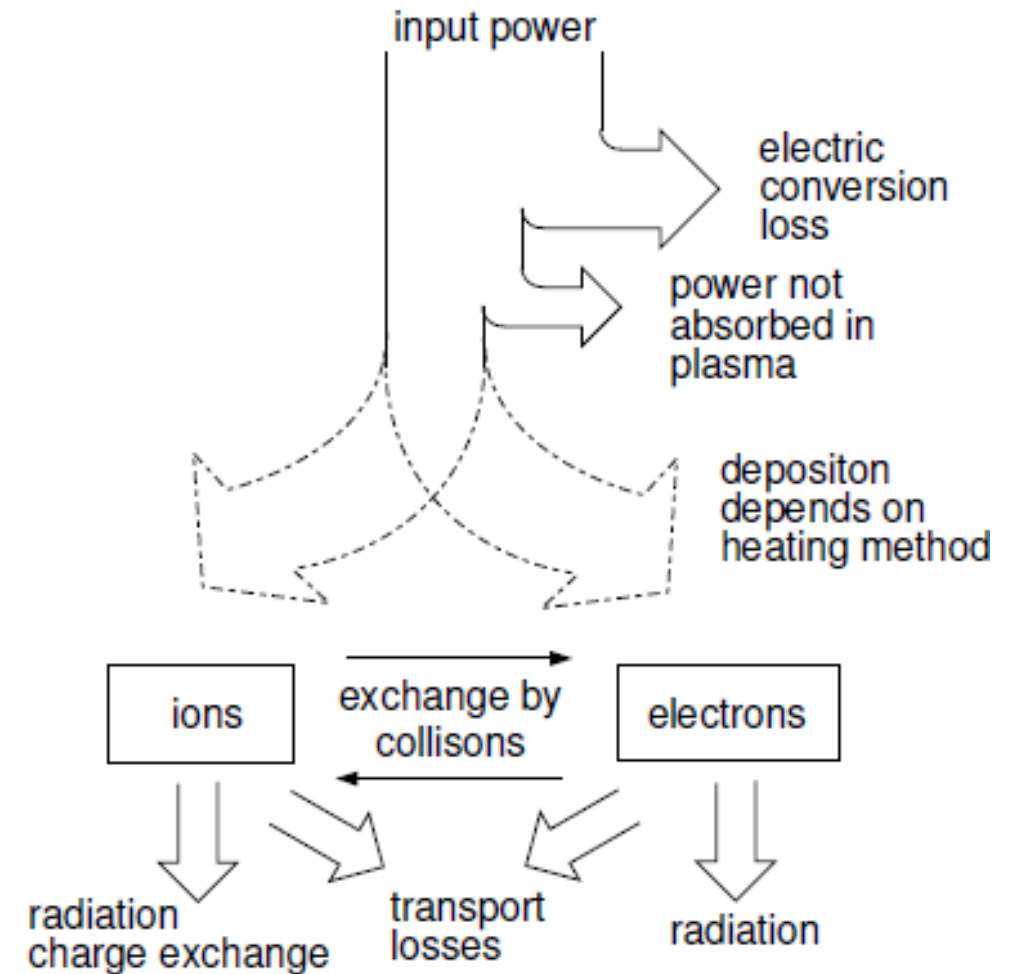
June 14th, 2024

Material from: various S.J. Diem SULI lectures, other talks as noted & J. Coehn NE 536 course at UW-Madison

Current drive and heating required to achieve fusion ignition conditions



$$Q = \frac{P_{fusion}}{P_{heat}}$$



Current drive and heating required to achieve fusion ignition conditions

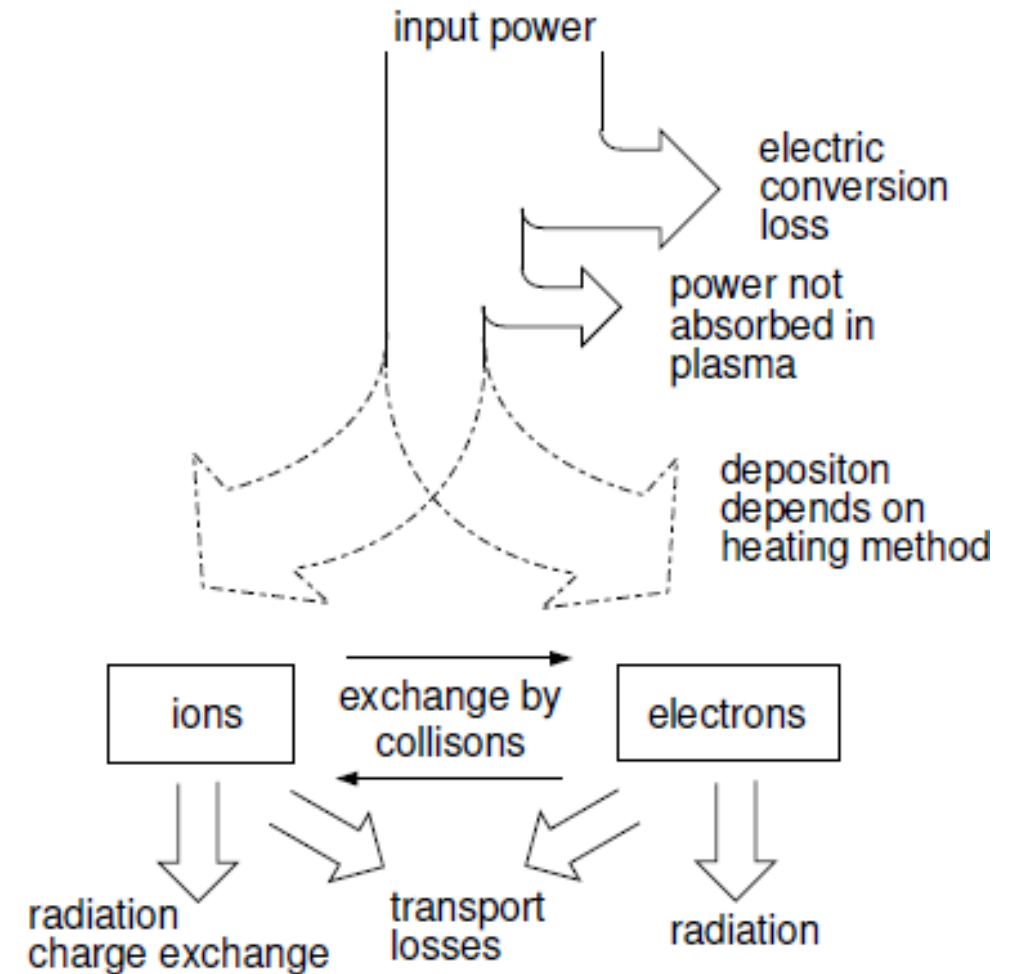
- Reaching ignition requires threshold for:

$$nT\tau_E > 2 \times 10^{21} \text{ m}^{-3}\text{-keV-s}$$

~ $2\text{-}3 \times 10^{20}$ ions/ m^3

~1-2 seconds

~100-200 million K



Current drive and heating required to achieve fusion ignition conditions

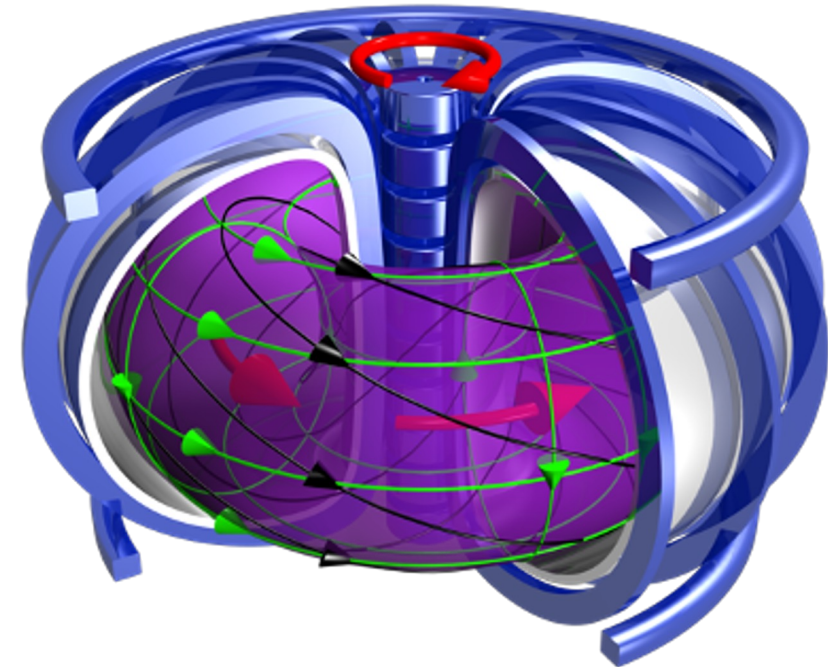
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Tokamak: External fields + plasma current to generate confining field



Plasmas require heating and current drive to achieve fusion conditions

- Reaching ignition requires threshold for:

$$n \cdot T \cdot \tau_E$$

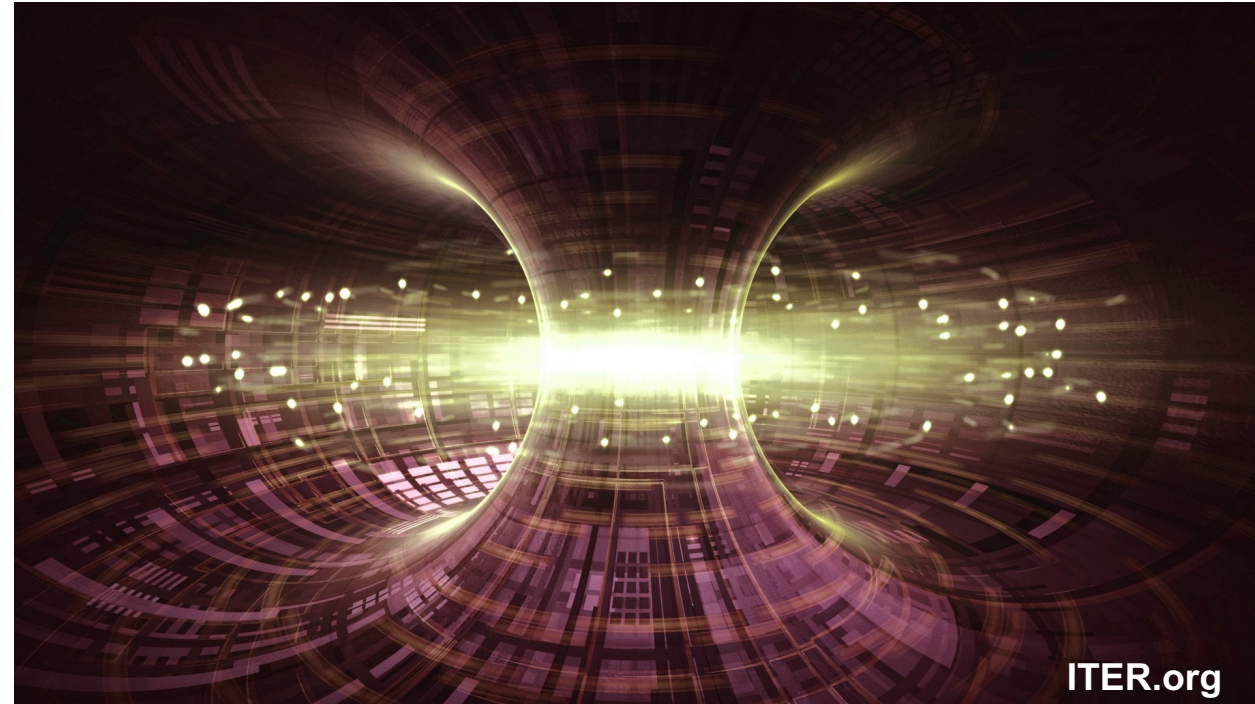
- External heating required to reach temperature for ignition
- After ignition, self-heating sustains plasma
- Several methods of external heating & current drive available
 - Ohmic heating**
 - Neutral beam injection**
 - Electron cyclotron resonance heating**
 - Lower hybrid resonance heating
 - Ion cyclotron resonance heating

	Fusion Gain	α -Heating Fraction	Scientific Frontier
	$Q = \frac{P_{fusion}}{P_{heat}}$	$f_{\alpha} = \frac{P_{\alpha}}{P_{\alpha} + P_{heat}}$	
Scientific Breakeven	Q = 1	17%	Alpha confinement
Burning Plasma Regime	Q = 5	50%	Alpha heating; Alpha effects on energetic particle instabilities
	Q = 10	67%	Strong alpha heating; Non-linear coupling effects
	Q = 20	80%	Burn Control; potentially strong non-linear coupling
	Q = ∞	100%	Ignition

From C. Collins

Auxiliary plasma heating required for fusion energy

- Burning plasmas will be heated by alpha particles produced through fusion – but they don't start out that way
- Auxiliary heating power required for: plasma initiation and current ramp up
- Need to heat plasma towards fusion conditions, provide burn control
 - Control MHD instabilities
 - Control against impurity radiation
 - Control plasma profiles
- **Can also provide current drive for long pulse or steady state operation**



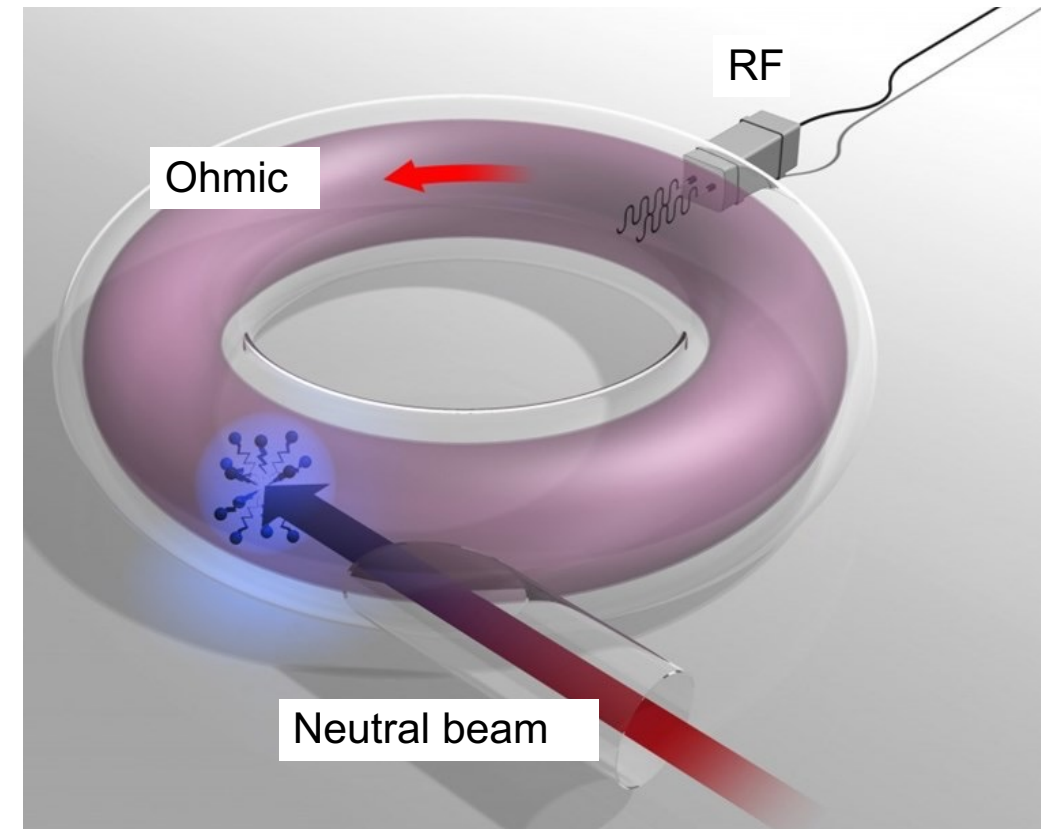
ITER.org

Plasmas require heating and current drive to achieve fusion conditions

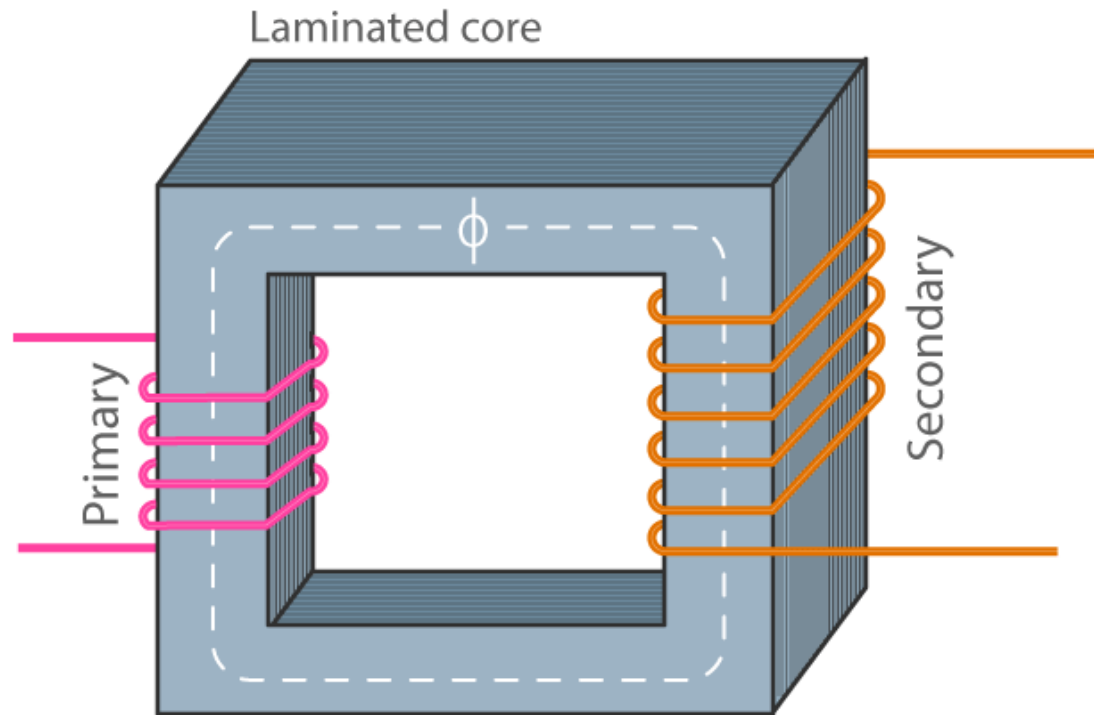
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Ohmic heating - like a transformer



Maxell-Faraday equation

$$\oint \vec{E} \cdot d\vec{l} = -\frac{\partial}{\partial t} \int \vec{B} \cdot d\vec{S}$$

Magnetic field of a solenoid

$$B = \frac{\mu_0 \mu_r N}{L} I$$

© Byjus.com

Toroidal electric field:

$$2\pi R E_\phi = -\frac{\mu_0 N A}{L} \frac{\partial I}{\partial t}$$

Ohmic heating – like a really, really, large transformer



Simplified Ohm's law:

$$\bar{E} + \bar{v} \times \bar{B} = \eta \bar{J}$$

Assume a stationary plasma, take curl of Ohm's law:

$$\nabla \times \bar{E} = -\frac{\partial \bar{B}}{\partial t} = \nabla \times (\eta \bar{J})$$

Take curl, assume η is constant

$$-\frac{\partial}{\partial t} \nabla \times \bar{B} = \eta \nabla \times \nabla \times \bar{J} = \eta [\nabla(\nabla \cdot \bar{J}) - \nabla^2 \bar{J}]$$

Diffusion equation for current:

$$\frac{\partial \bar{J}}{\partial t} = \frac{\eta}{\mu_0} \nabla^2 \bar{J}$$

Current evolution in tokamaks

For resistivity not a constant, then

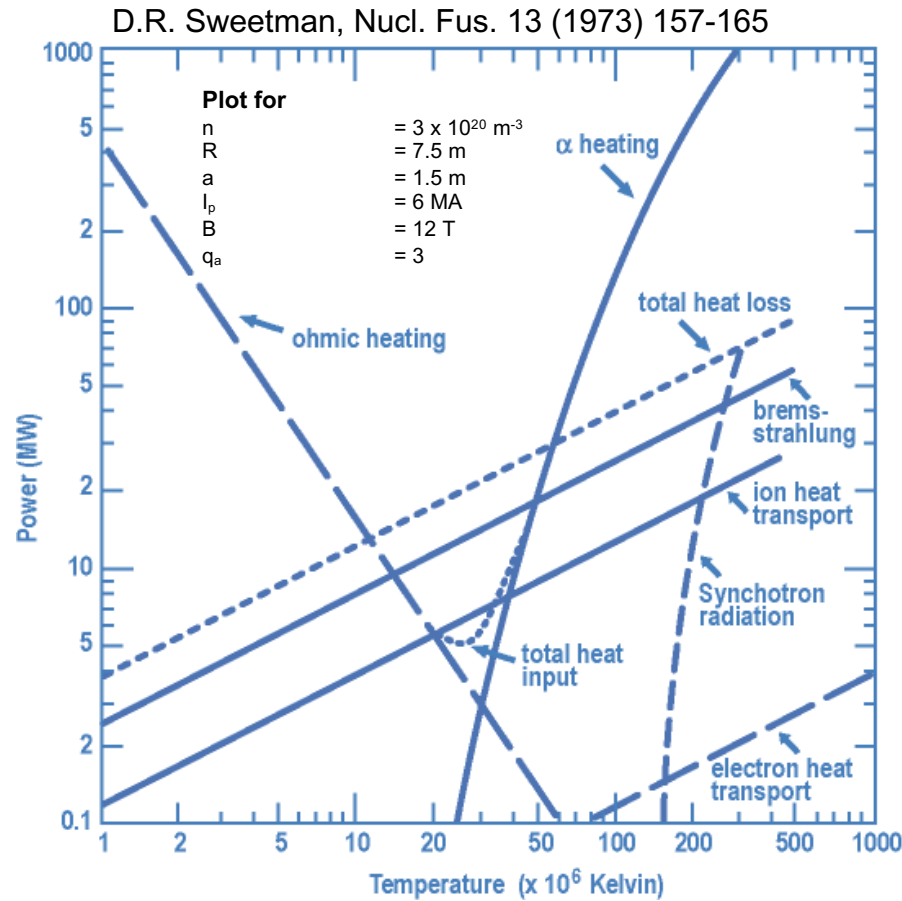
$$-\frac{\partial \bar{J}}{\partial t} = \frac{1}{\mu_0} \nabla^2 (\eta \bar{J}) - \nabla [\nabla \cdot (\eta \bar{J})]$$

Take toroidal component of the above equation:

$$-\frac{\partial J_\phi}{\partial t} = \frac{1}{\mu_0} \nabla^2 (\eta \bar{J}_\phi)$$

- Current initially driven at surface, then quickly diffuses into plasma
- Resistive heating raises ηJ^2 temperature
- As discharge evolves, current diffuses into plasma core

Ohmic heating can only do so much – there's a limit



Plasma current is limited in tokamaks

$$j \leq \frac{B_\phi}{\mu_0 R}$$

- Plasma resistivity
- Dissipated power
- Plasma stability requires

$$\eta \propto T_e^{-3/2}$$

$$p = \eta \cdot j^2$$

Having to balance Ohmic heating with

$$q_a = \frac{aB_\phi}{RB_\theta} \geq 2$$

Means plasma is limited to a few keV

$$P_{rad,brems} / V = 5.35 \times 10^{-37} \cdot (n_e / \text{m}^{-3})^2 \cdot Z_{eff} \cdot \sqrt{T / \text{keV}} \quad [\text{W} / \text{m}^3]$$

We need auxiliary heating

Ohmic engineering limits

- Requires time varying current – limits how much current can be driven
- Running current through a solenoid produces heat, limiting how long you can run it
- Ohmic current drive, heating limited to short pulses
 - Cannot be used for long times, steady-state
 - Can be used for plasma startup
- Critical challenge for spherical tokamaks: find a path to operate without an ohmic solenoid
 - Limited space for shielding
 - Drives need for solenoid-free startup



Pegasus-III: Going solenoid free allows more space for TF coils



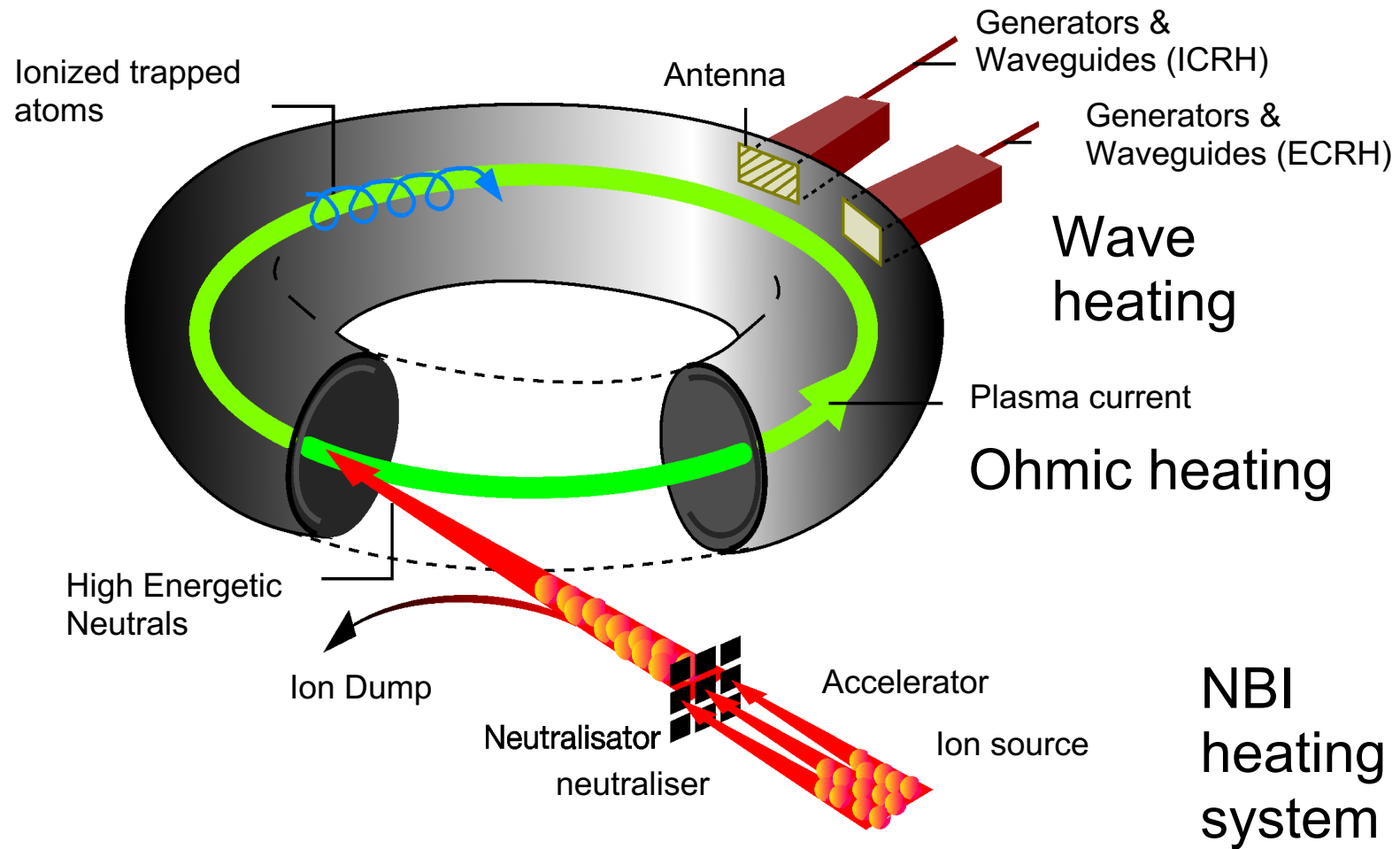
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Plasma auxiliary heating



Overview of plasma heating

- Ohmic heating
 - $P = V_{\text{loop}} * I_{\text{plasma}}$
 - Dissipative heating of current
 - Heats electrons
- Neutral beam injection (NBI)
 - Injection of high energetic neutral fuel atoms into plasma
 - Heating electrons and ions
- Electron cyclotron resonance heating
 - Inject microwaves with $\omega = \omega_{ce}$
 - Heats electrons
- Lower hybrid resonance heating
 - Inject waves with $\omega = (\omega_{ce}\omega_{ci})(1/2)$
 - Heats electrons and ions
- Ion cyclotron resonance heating
 - Injection of radio frequency waves with $\omega = \omega_{ci}$ (10s of MHz)
 - Heats ions





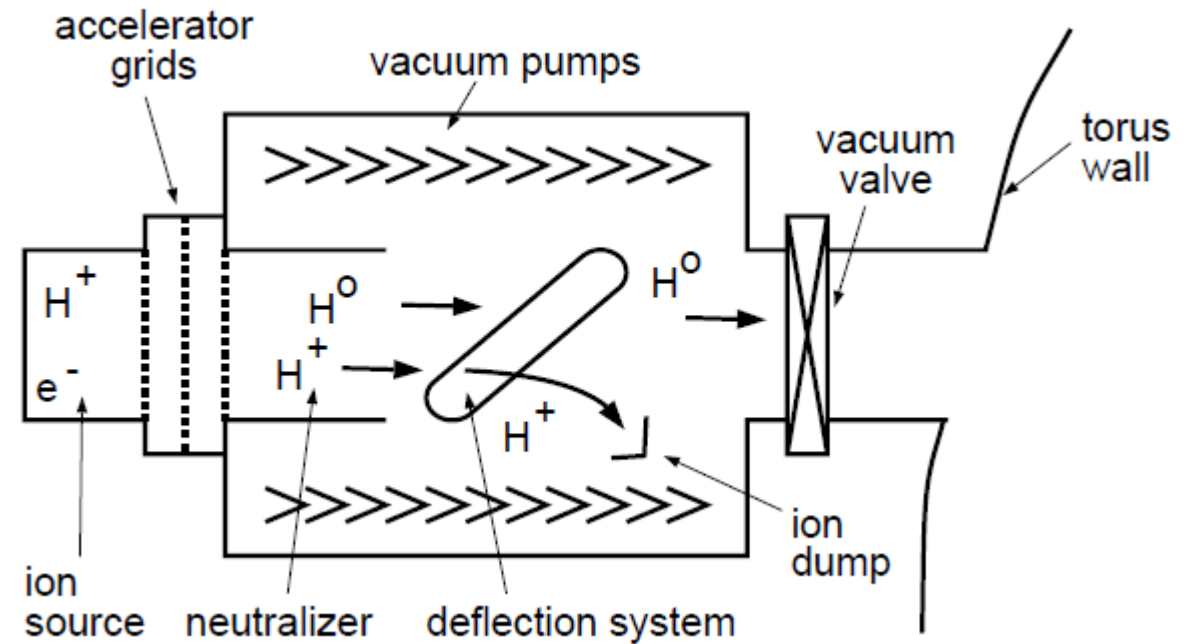
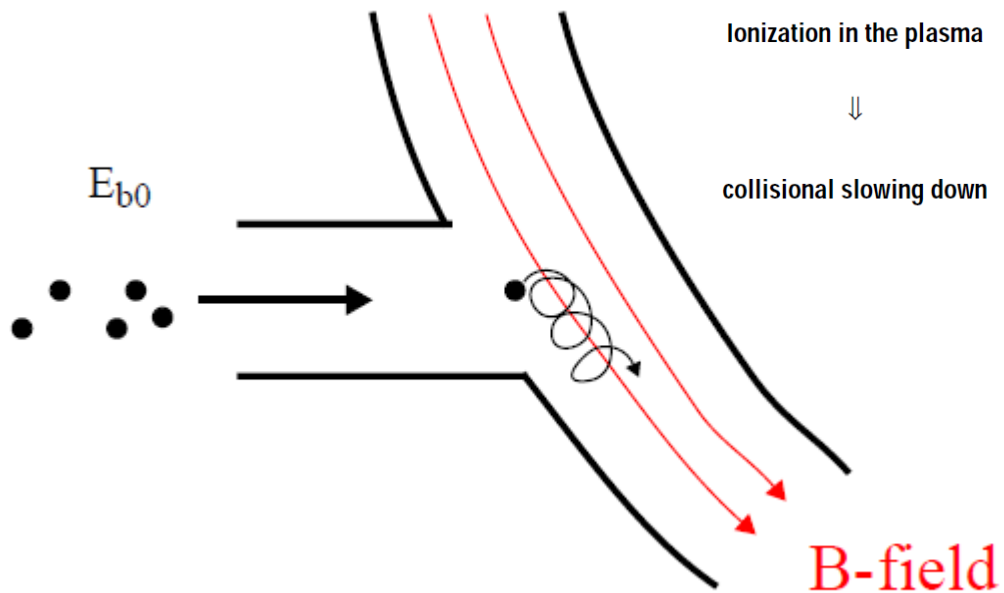
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Neutral beam injection



Heating with neutral beam injection – process overview

Injection of a beam of **neutral** fuel atoms (H, D, T) with high energies ($E_b > 50$ keV)



TEXTOR NBI: up to 60 keV, 40 A neutral current, $P_{in} = 2$ MW
Co / counter beams

Neutral beam injection

An energetic neutral particle beam is injected and is thus transferring energy into the plasma

- via ionization and subsequent thermalization / coulomb collisions:
 - $H_{Beam} + e \rightarrow H^+ + e + e$ (electron collisions)
 - $H_{Beam} + p \rightarrow H^+ + e + p$ (ion collisions)
- via charge exchange and subsequent thermalization / coulomb collisions :
 - $H_{Beam} \text{ (fast)} + p_{Plasma} \text{ (slow)} \rightarrow H^+ \text{ (fast)} + H \text{ (slow)}$

All three reactions play a role when considering the penetration depth into the plasma:

$$\frac{dI_{Beam}}{dx} = -n \left(\sigma_{cx} + \sigma_{ion,i} + \frac{\langle \sigma_{ion,e} v_e \rangle}{v_{Beam}} \right) I_{Beam}$$

Neutral beam injection

Penetration depth

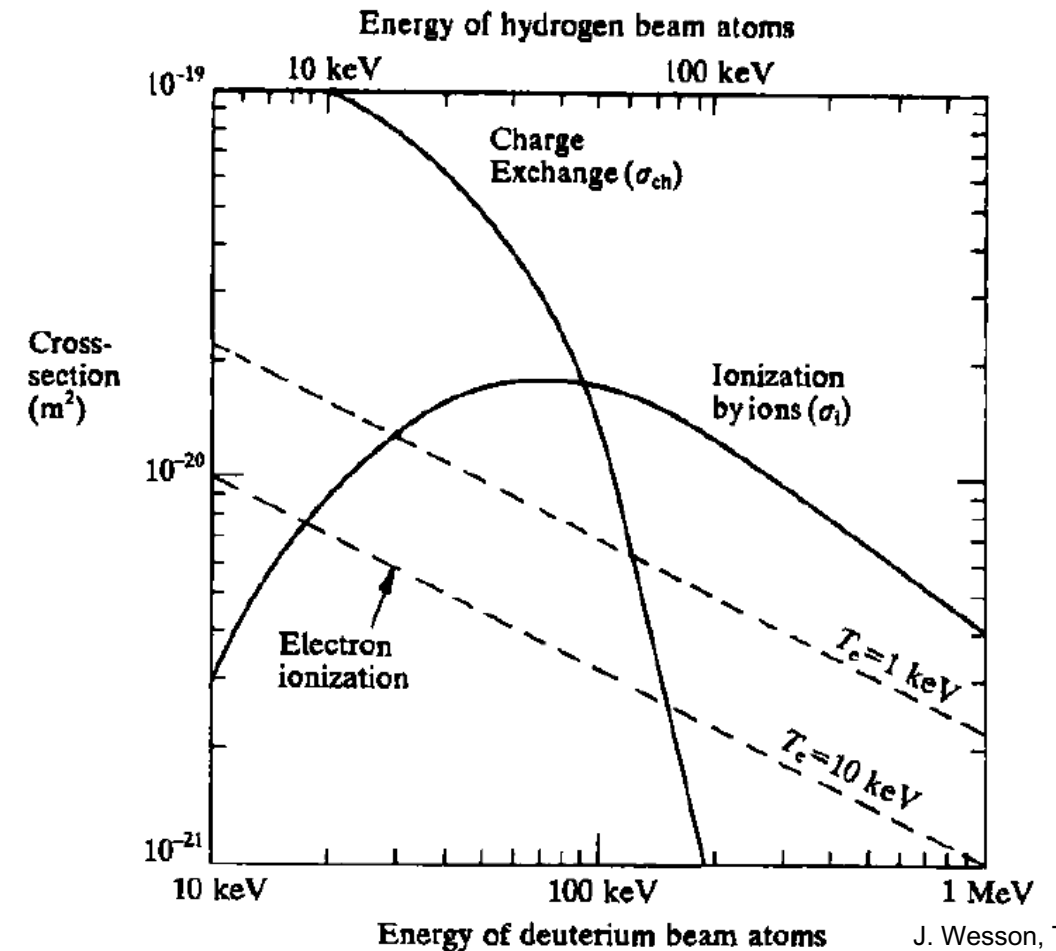
All three reactions play a role when considering the penetration depth into the plasma:

$$\frac{I_{Beam}(x)}{I_{Beam,0}} = e^{-n \left(\sigma_{cx} + \sigma_{ion,i} + \frac{\langle \sigma_{ion,e} v_e \rangle}{v_{Beam}} \right) x}$$

Beam attenuation also caused due to

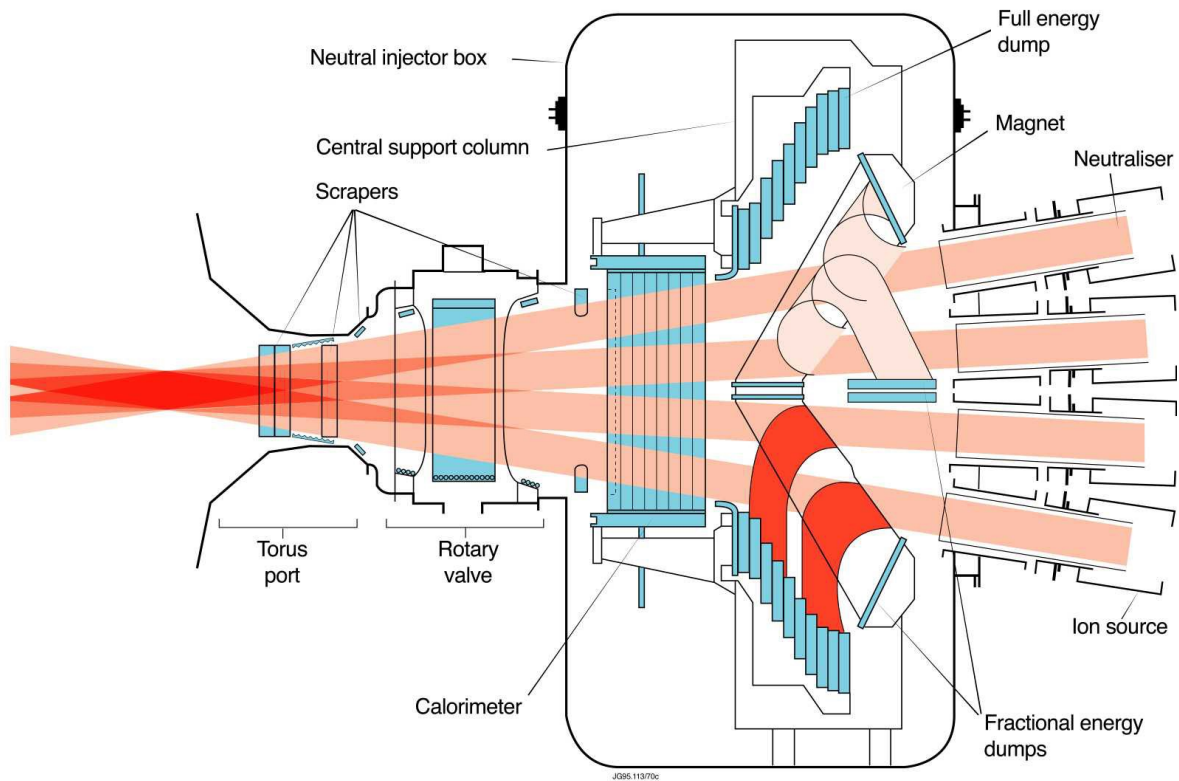
- elastic collisions with plasma species
- collisions with impurities

→ Further decrease of penetration depth

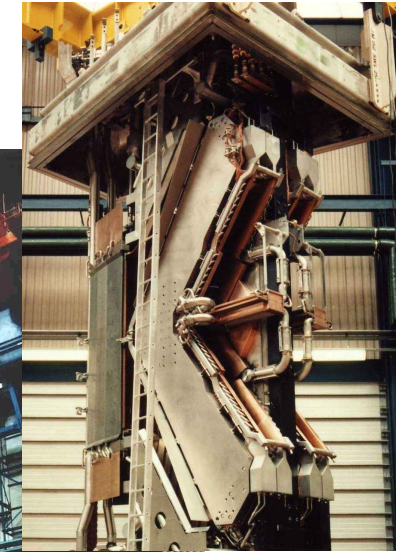


J. Wesson, Tokamaks

JET neutral beam system & components



JET NB Injector cryopump



JET NB deflection magnet, residual ion dumps and calorimeter

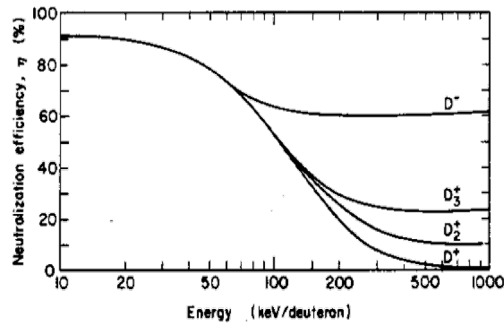


Neutral Beam Injection

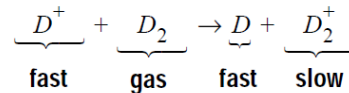
Particle Energies and Physical Limits

- Problem for reactor NBI
 - Higher particle energies required (1 MeV for ITER)
 - neutralization efficiencies drop for higher energies
- Solution: Negative Ions

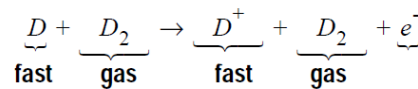
Efficiency:



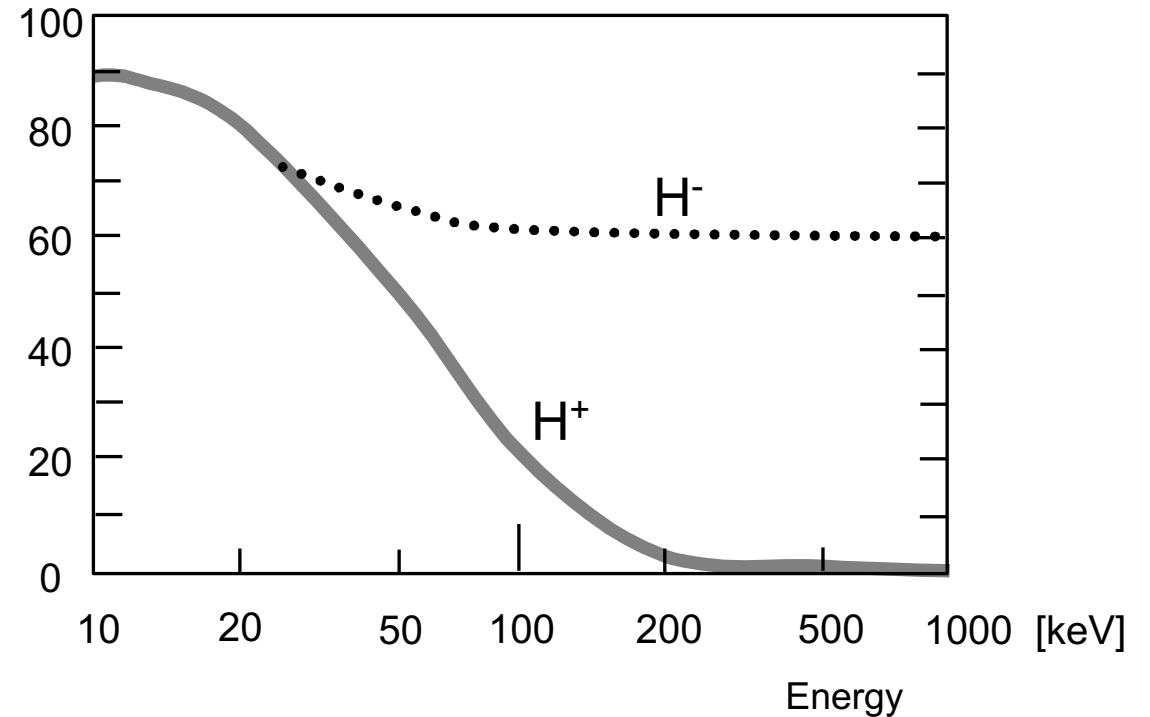
based on **charge exchange**



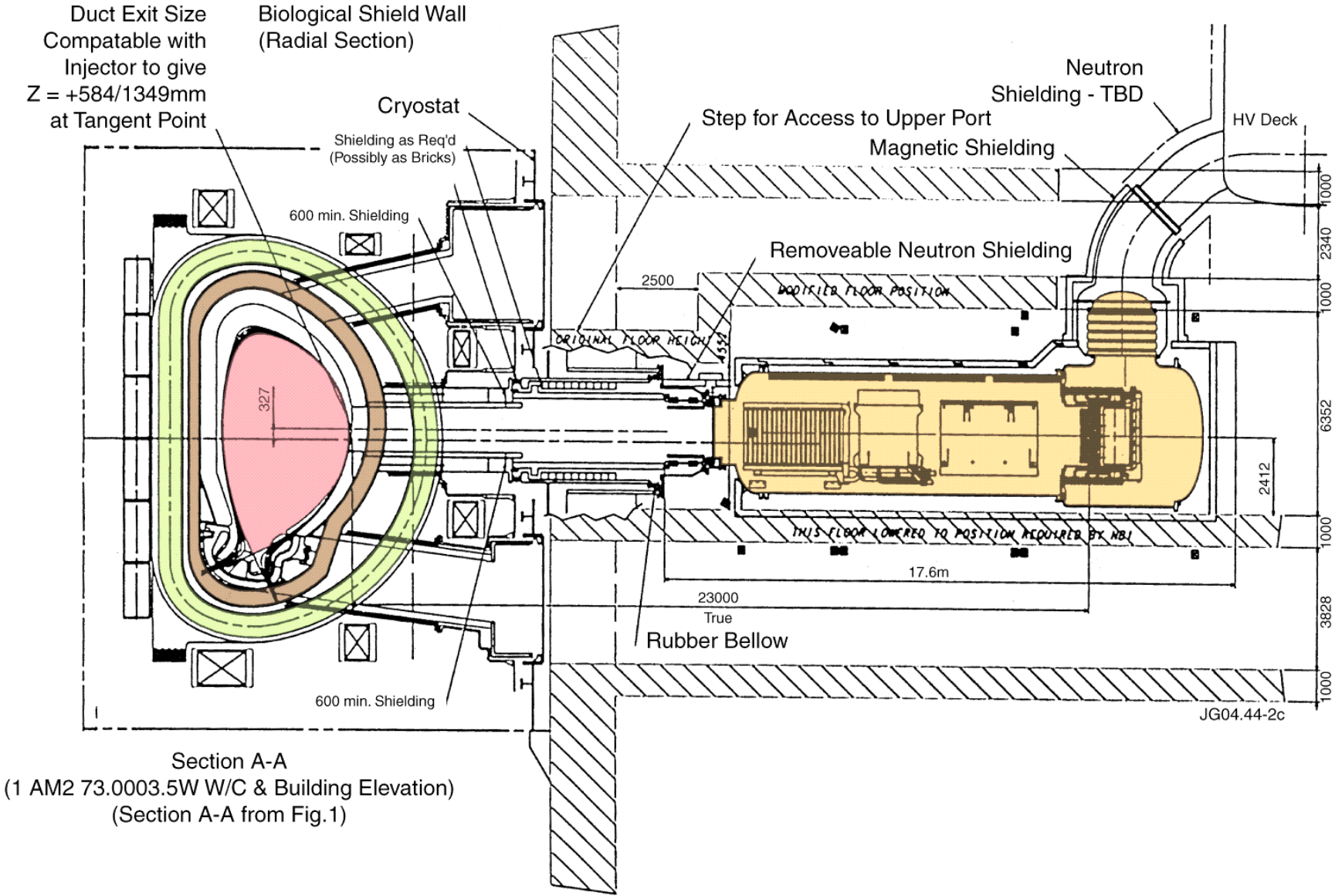
balance against **re-ionization**



Neutralisation efficiency



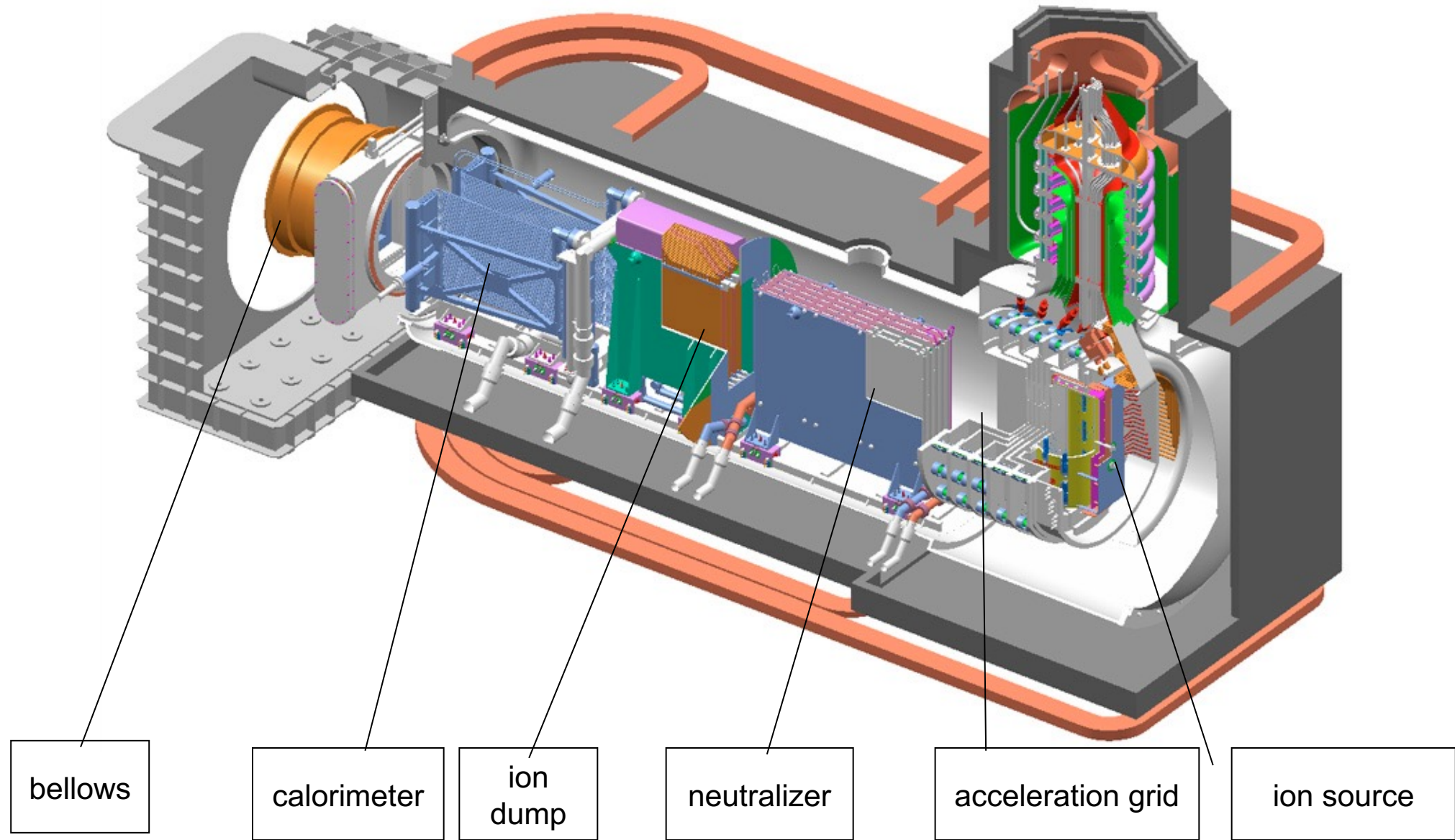
ITER NBI beamline



Section A-A
 (1 AM2 73.0003.5W W/C & Building Elevation)
 (Section A-A from Fig.1)

Neutral particle injector for ITER

$E = 1 \text{ MeV}$
 $P = 2 \times 16.5 \text{ MW}$





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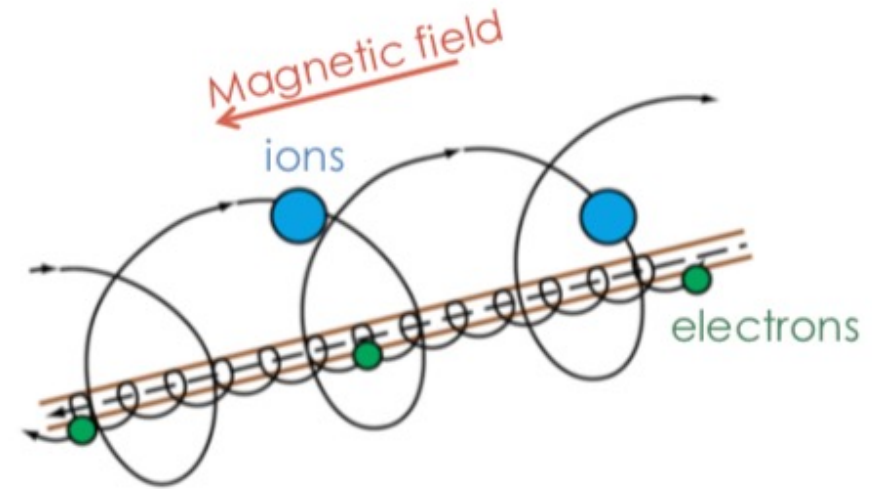
Microwave heating



Electron cyclotron range waves provide heating, drive current

- Electron cyclotron (EC) frequency is the natural frequency of rotation of electrons in magnetic fields

$$f_{ce} = \frac{eB}{2\pi m_e c}$$



$$F = q(\cancel{E} + v \times B)$$

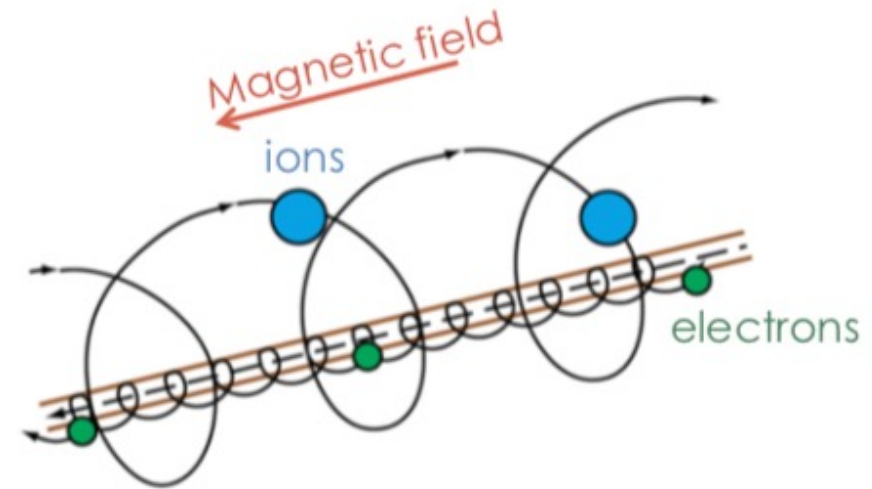
CYCLOTRON MOTION

Electron cyclotron range waves provide heating, drive current

- Electron cyclotron (EC) frequency is the natural frequency of rotation of electrons in magnetic fields

$$f_{ce} = \frac{eB}{2\pi m_e c}$$

- Considering this frequency range, there are two solutions to the cold plasma dispersion relation
- Ordinary mode (O-mode)
 - E is parallel to B
 - Independent of B
 - Depends on density
- Extraordinary mode (X-mode)
 - E is perpendicular to B
 - Depends on B, n_e



$$F = q(\cancel{E} + v \times B)$$

CYCLOTRON MOTION

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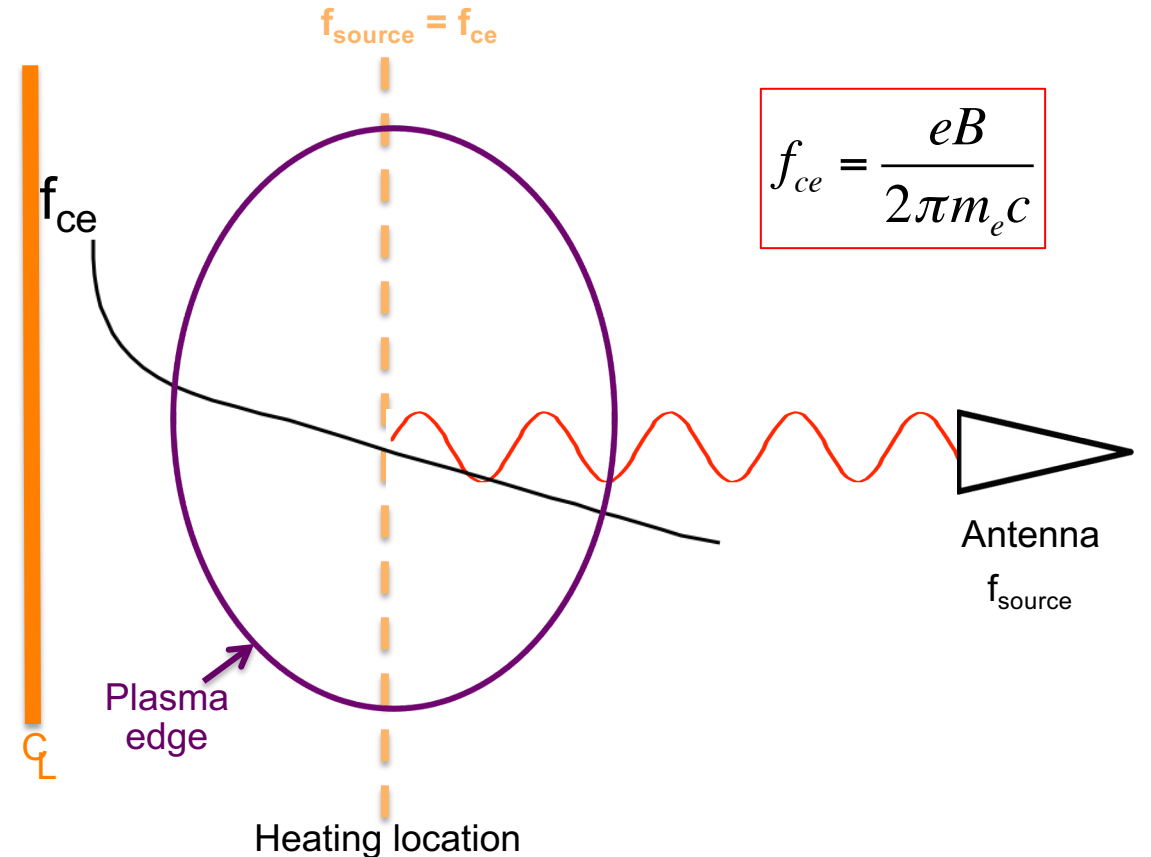
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 - E is perpendicular to B
 - Depends on B, n_e

Both O-mode and X-mode have resonances at the electron cyclotron frequency, cutoffs depend on plasma density

EC waves provide localized heating/current drive

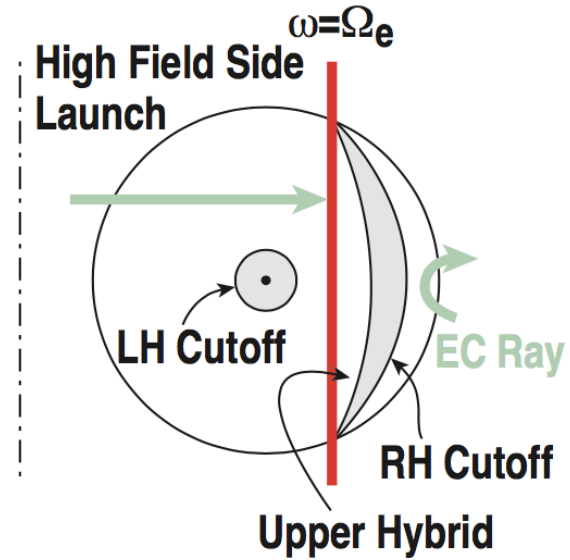
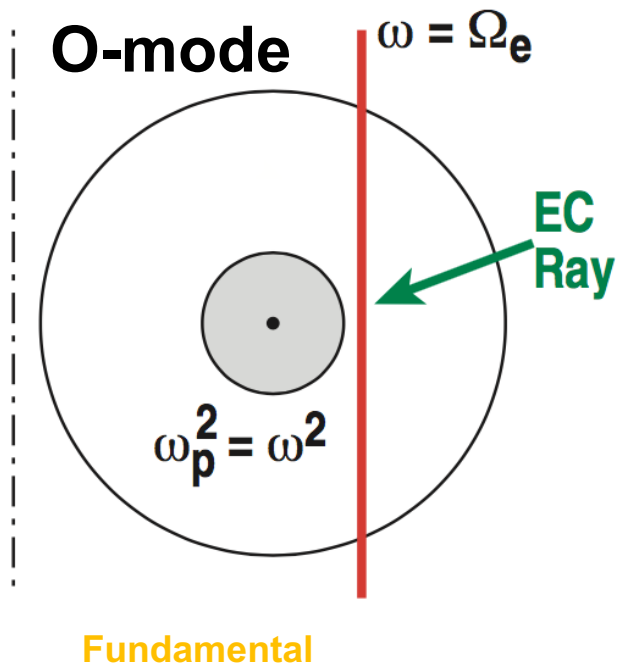
- Launched radiofrequency (RF) waves absorbed near cyclotron resonance
 - Tune to either electron or ion cyclotron motion
 - RF source frequency can be chosen to heat precise radius
 - For tokamaks, $B_t \propto 1/R$



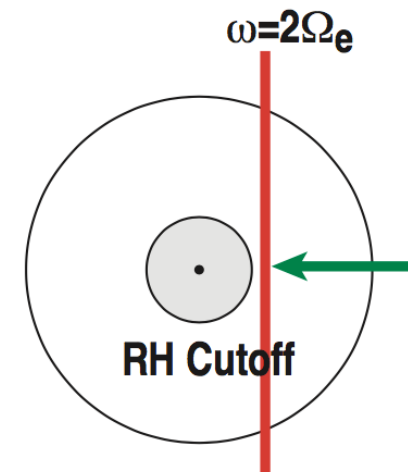
EC waves provide localized heating/current drive

- Can provide:
 - Electron heating
 - Current profile control, sustainment
 - Control of magnetohydrodynamic (MHD) activity

X-mode



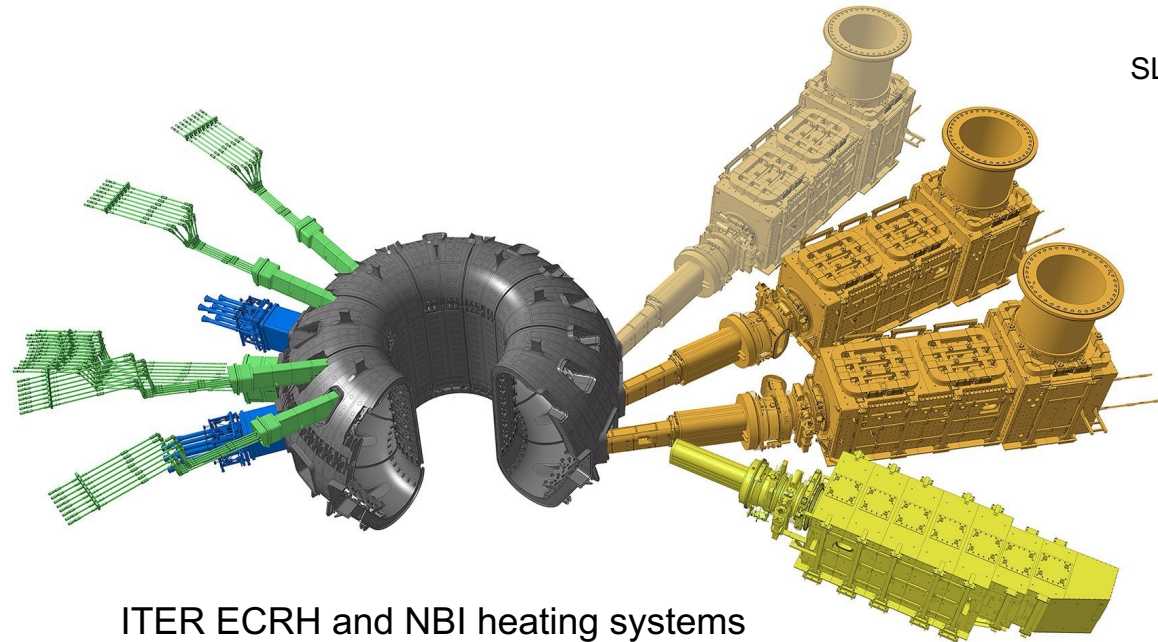
Fundamental



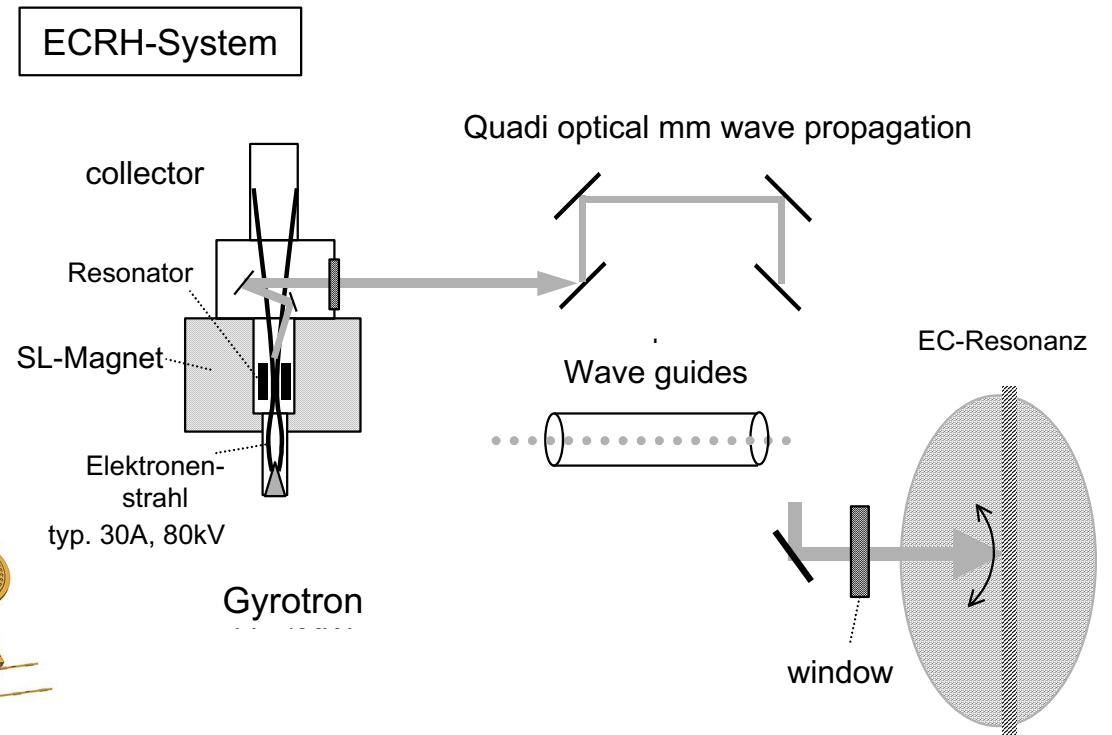
Second Harmonic

Microwave systems can be located far from device

Couple to the plasma via waveguides or use quasi optical via mirrors using mm optics to bring waves into plasma

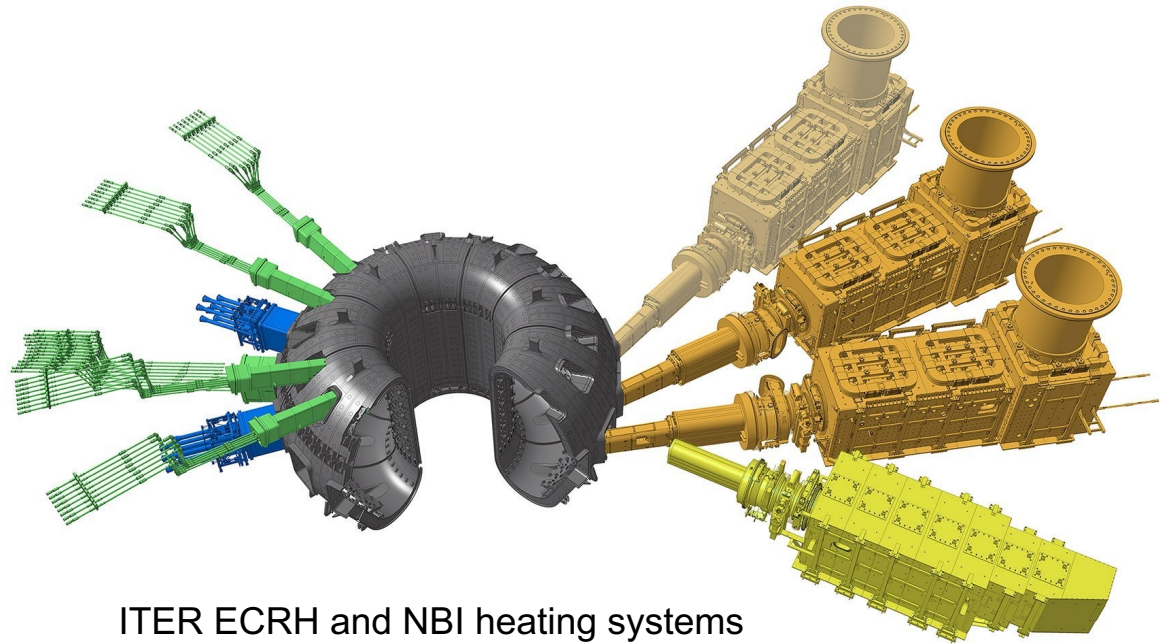


ITER ECRH and NBI heating systems



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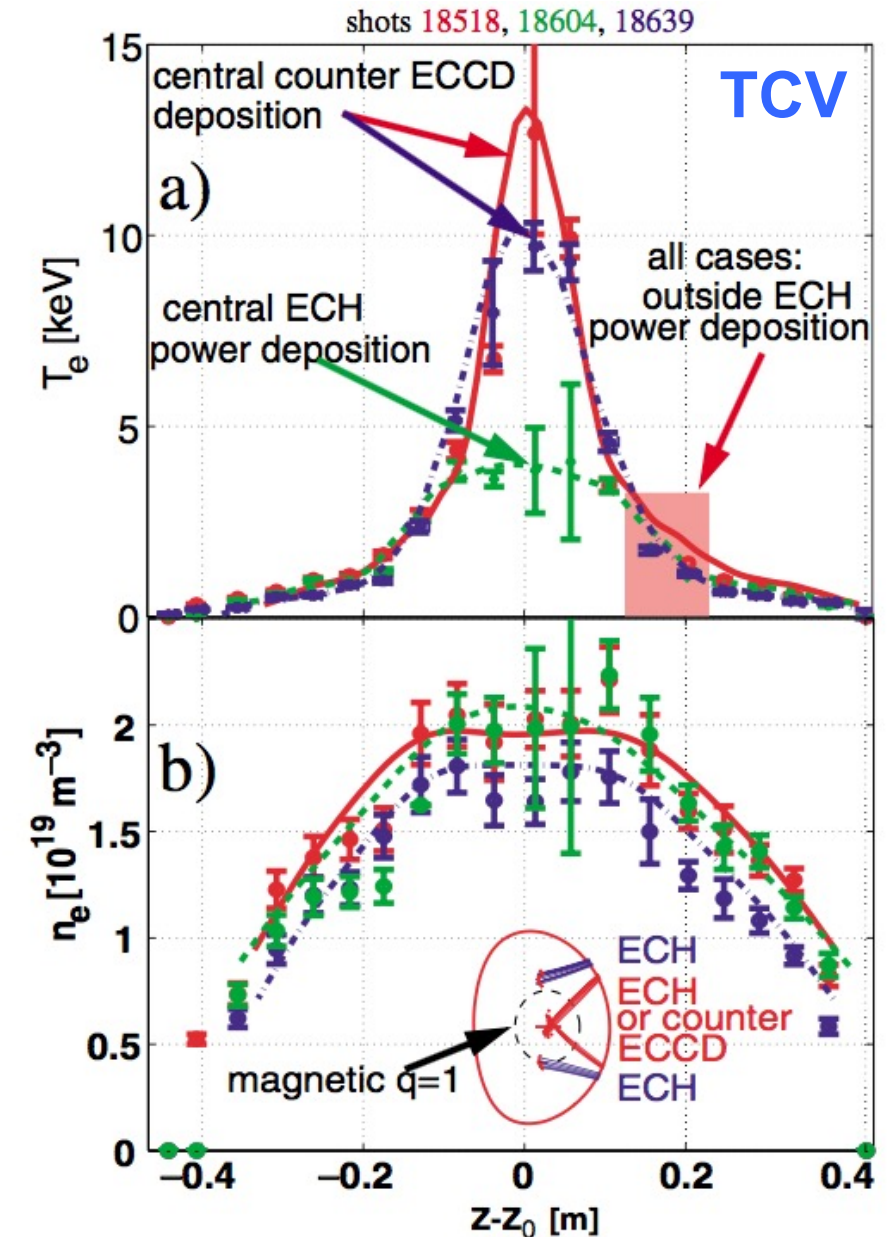
ITER ECRH and NBI heating systems



In the same ITER ECRH port plug

EC waves provide localized heating/current drive

- Many examples of ECH/ECCD in tokamaks and other confinement devices
 - Large-scale, high-performance devices depend on waves for heating
- EC heating/ EC current drive can provide current profile tailoring in TCV
 - Improve central electron energy confinement
 - Stabilize MHD modes

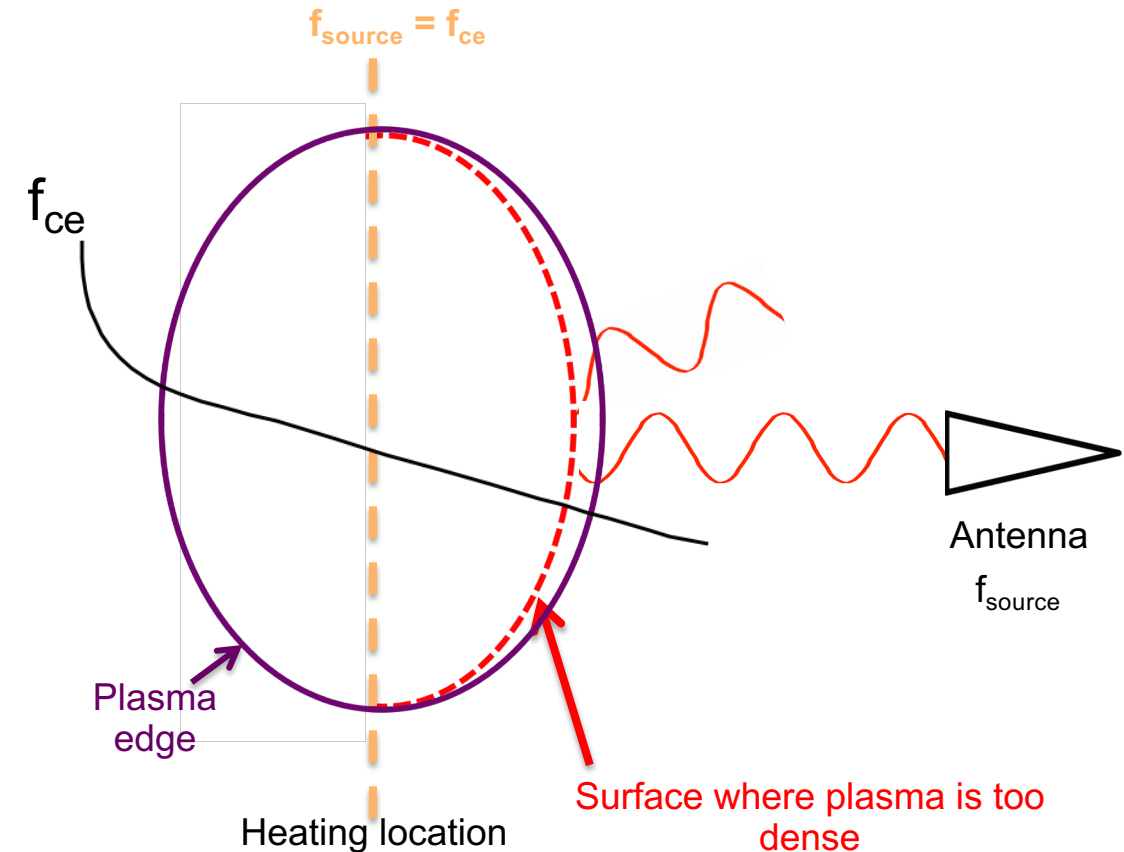


Electron cyclotron wave injection provides plasma heating, current drive – in certain conditions

- If plasma is too dense, O-mode and X-mode reflected near plasma edge
 - Happens in spherical tokamaks and stellarators

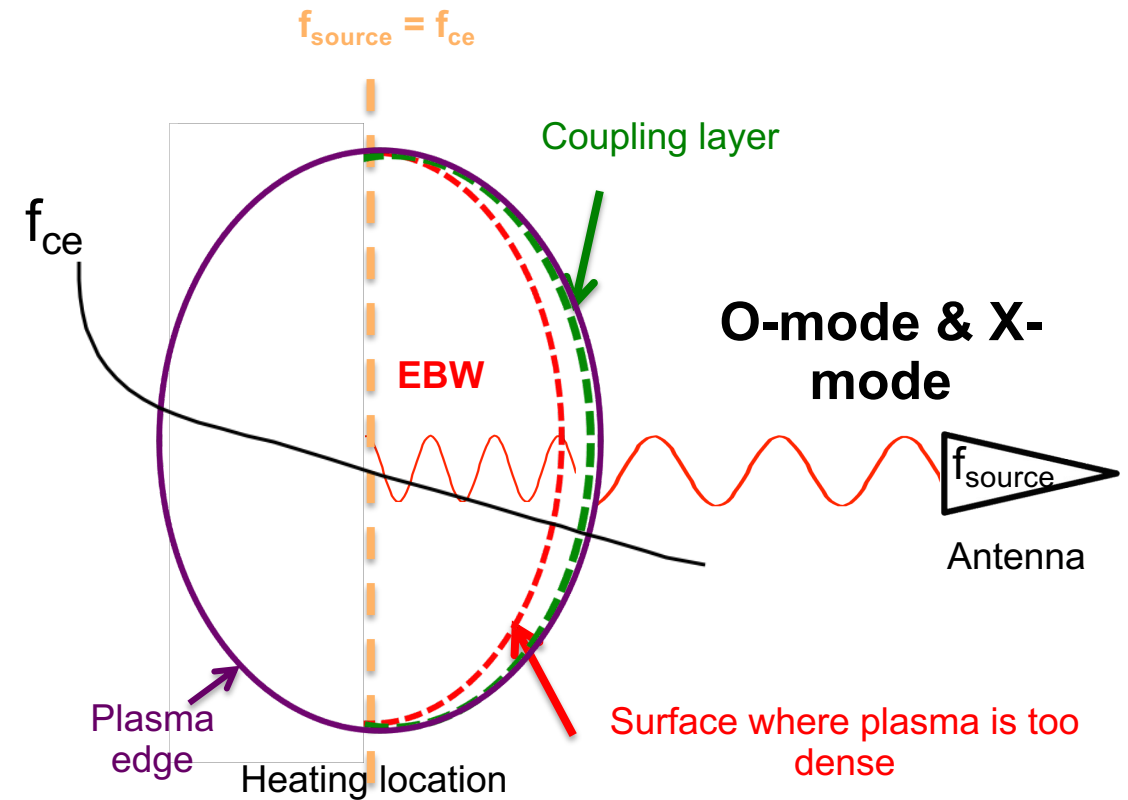
$$\omega_{\text{source}} > \omega_{\text{pe}}$$

- **Alternative heating method required**



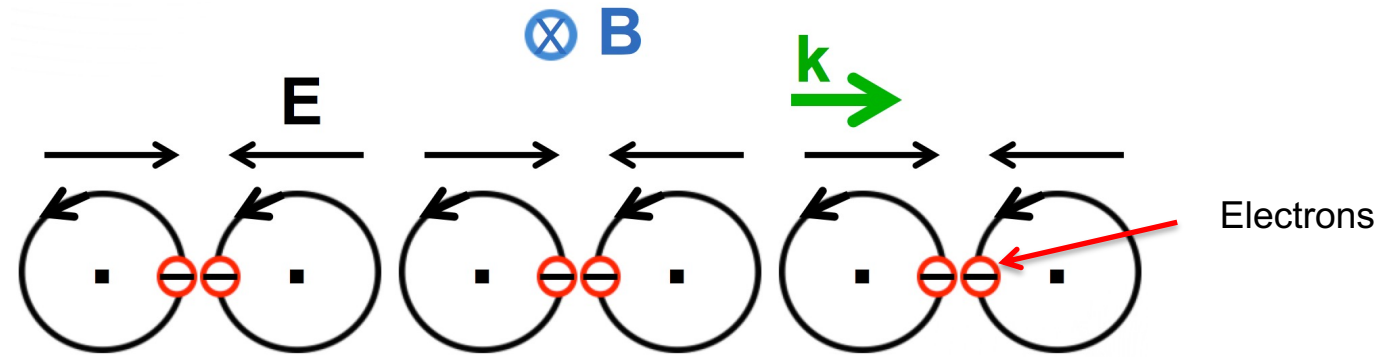
Electron Bernstein waves can travel in high density plasmas

- Electron Bernstein Waves (EBW) can only travel inside the plasma
 - Wave moves due to coherent motion of charged particles
- Can only couple to EBW by launching O- or X-modes



Electron Bernstein waves can propagate in overdense plasmas

- Electron Bernstein waves (EBW) are hot plasma waves:
 - Longitudinal, electrostatic waves
 - Propagates perpendicular to B
 - Do not experience a density cutoff in the plasma



- Cannot propagate in vacuum -> must launch O- or X-mode to mode couple to EBW

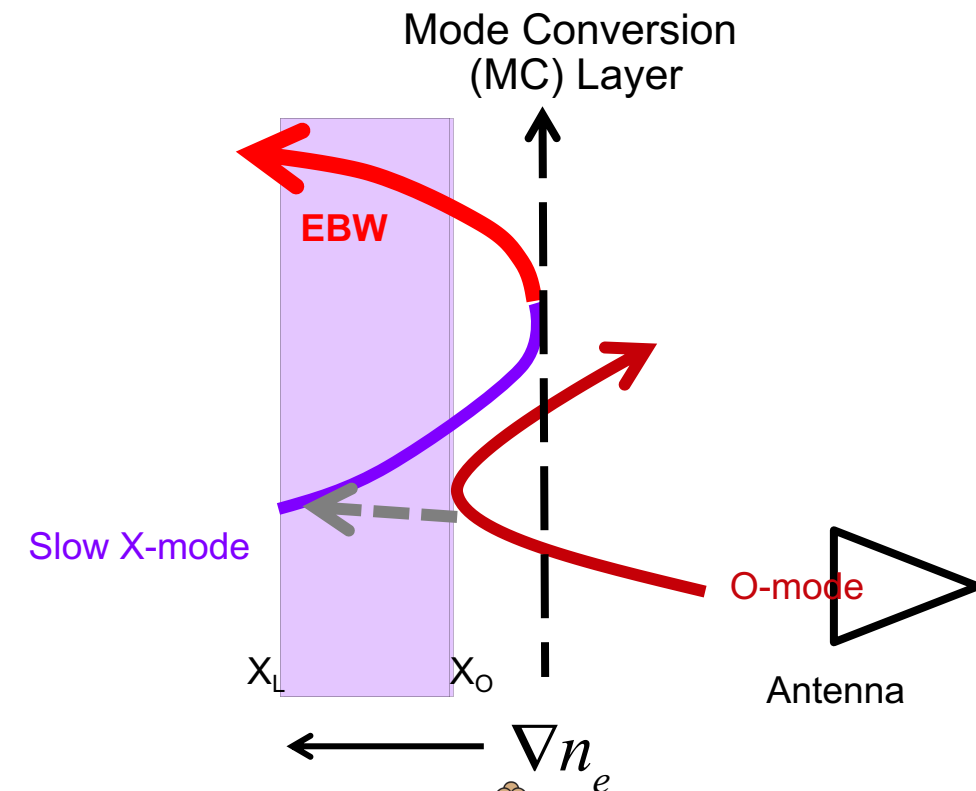
$$1 - 2 \sum_s \frac{4\pi n_s m_s c^2}{\lambda B_0^2} \left[\sum_s e^{-\lambda} I_n(\lambda) \frac{n^2}{\left(\frac{\omega}{\Omega}\right)^2 - n^2} \right] = 0 \quad \text{Where: } \lambda = \frac{k_{\perp}^2 k T_{\perp}}{m \Omega^2}$$

- As wave frequency approaches EC harmonic, $\omega = n\Omega_c$, wave is strongly absorbed

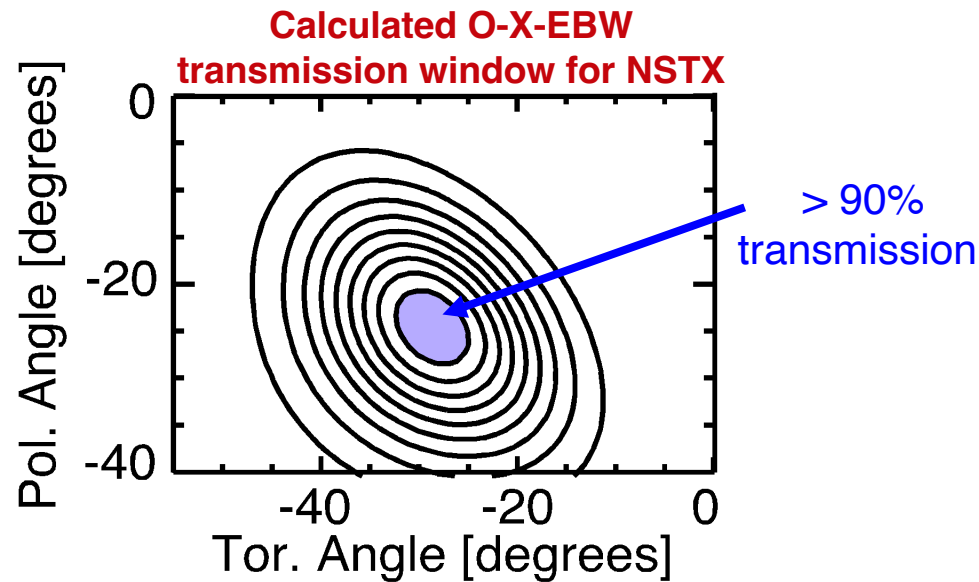
Electron Bernstein waves can propagate in overdense plasmas

- Electron Bernstein waves (EBW) are hot plasma waves:
 - Perpendicularly propagating, $k_{\parallel} = 0$
 - Do not experience a density cutoff in the plasma
 - Longitudinal, electrostatic waves
 - Cannot propagate in vacuum
 - Absorbed near cyclotron harmonics
- EBW coupling efficiency depends on plasma parameters near plasma edge
 - Density gradient
 - Magnetic field pitch

O-X-B Coupling

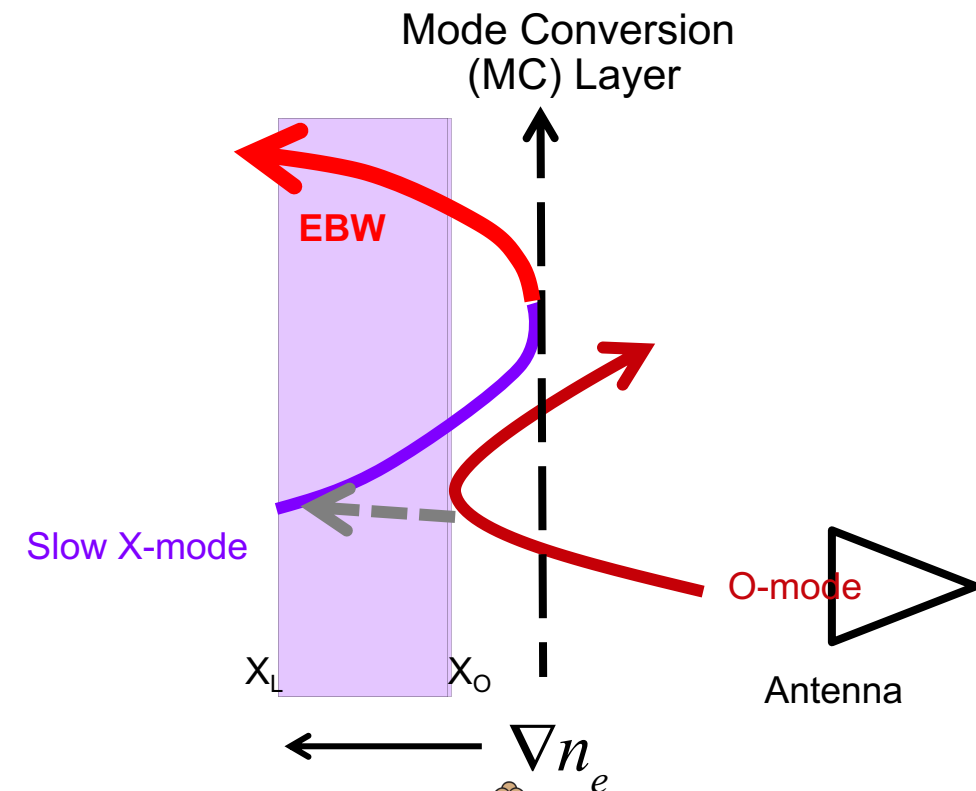


Electron Bernstein waves can propagate in overdense plasmas



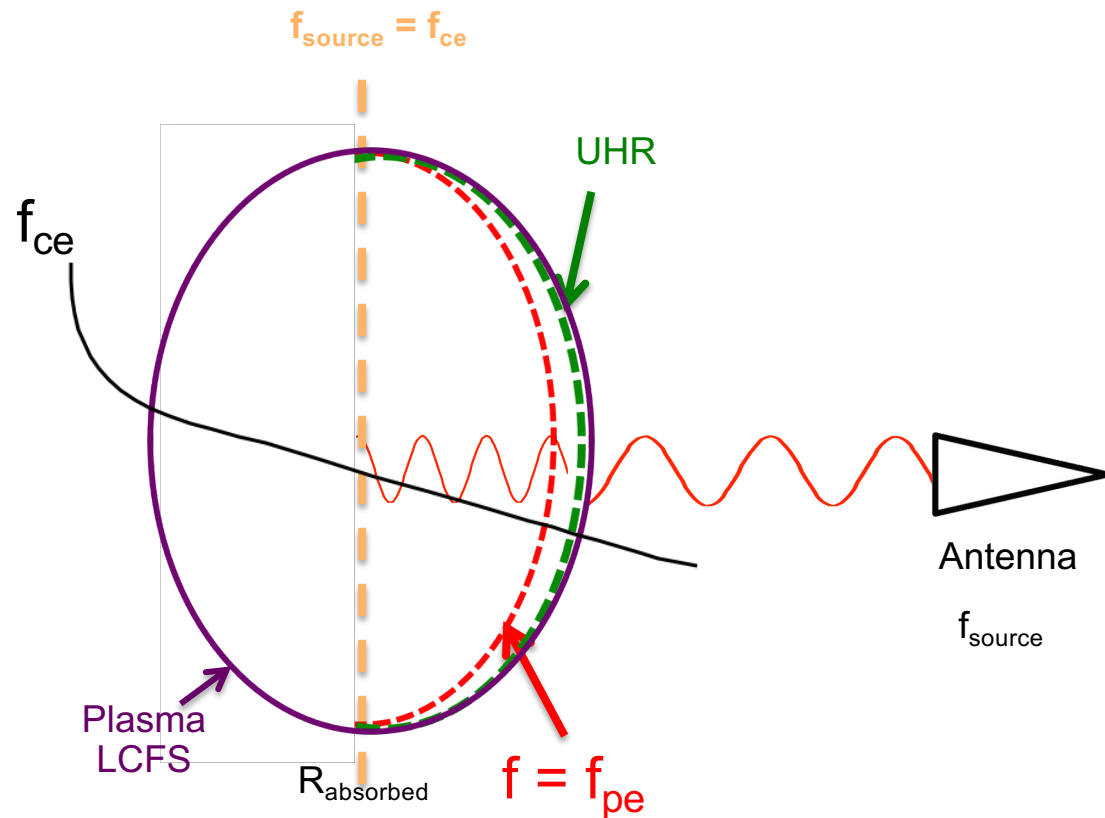
- EBW emission data can be used to provide coupling efficiency and polarization information to design heating, current drive system

O-X-B Coupling



EBW emission can be used to measure temperature

Electron Bernstein wave emission at blackbody levels, proportional to local T_e



Larmor formula:

$$I_{\omega} = \frac{\omega^2 k_B T_{\text{rad}}}{8\pi^3 c^2}$$

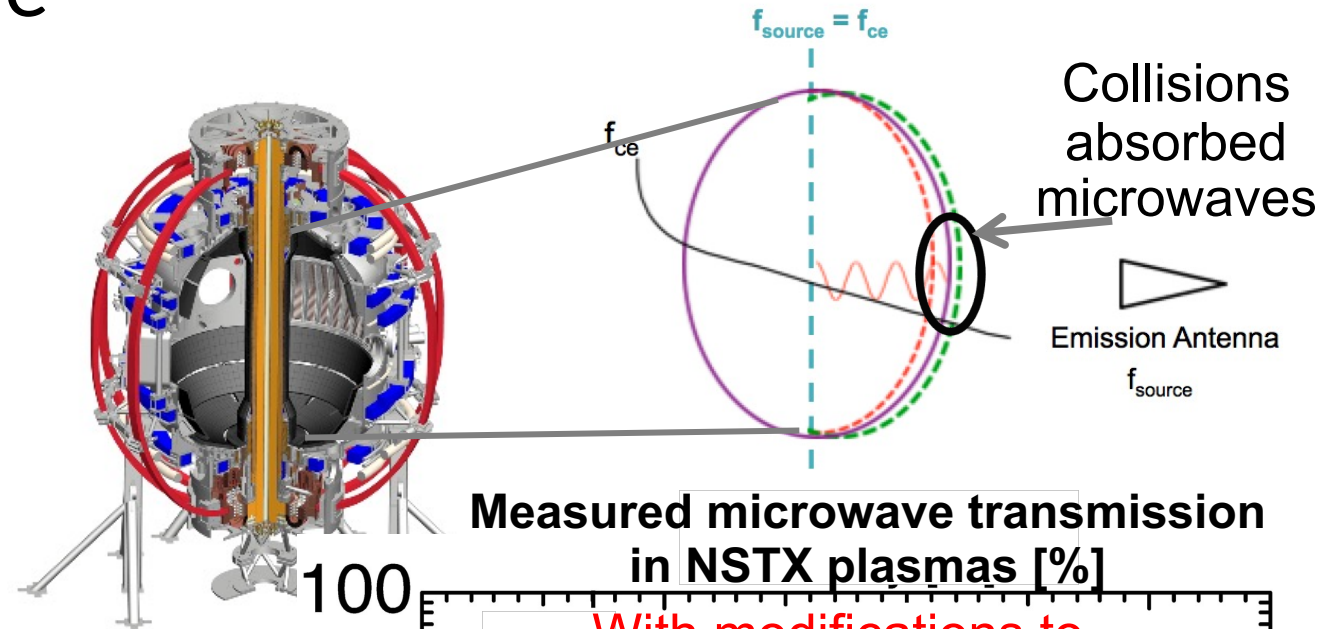
Measured T_{rad} is proportional to local T_e

$f_{\text{ce}} \sim 1/R \rightarrow$ radial localization

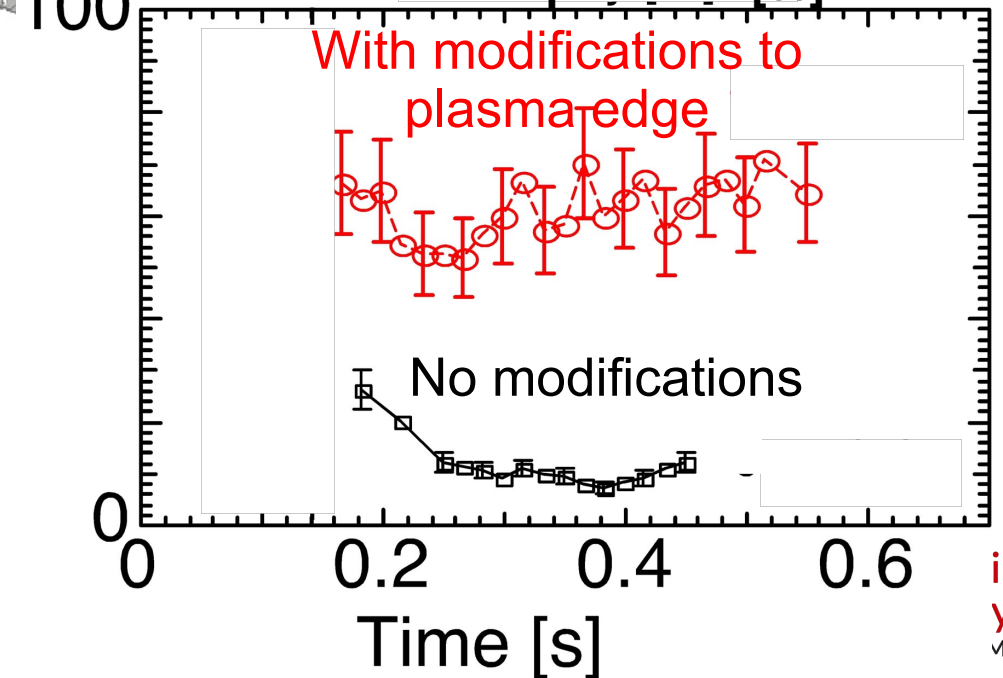
Diem et al, PRL (2009)

Coupling microwave power to high density fusion plasmas can be difficult - but possible

- Plasma naturally emits microwaves from cyclotron resonance location
- Assumed physics of microwave emission from high density plasmas same as launching
 - Measurements on NSTX didn't agree with predictions
 - Plasma edge had too many collisions, absorbed microwaves
- **Unexpected results present opportunities**

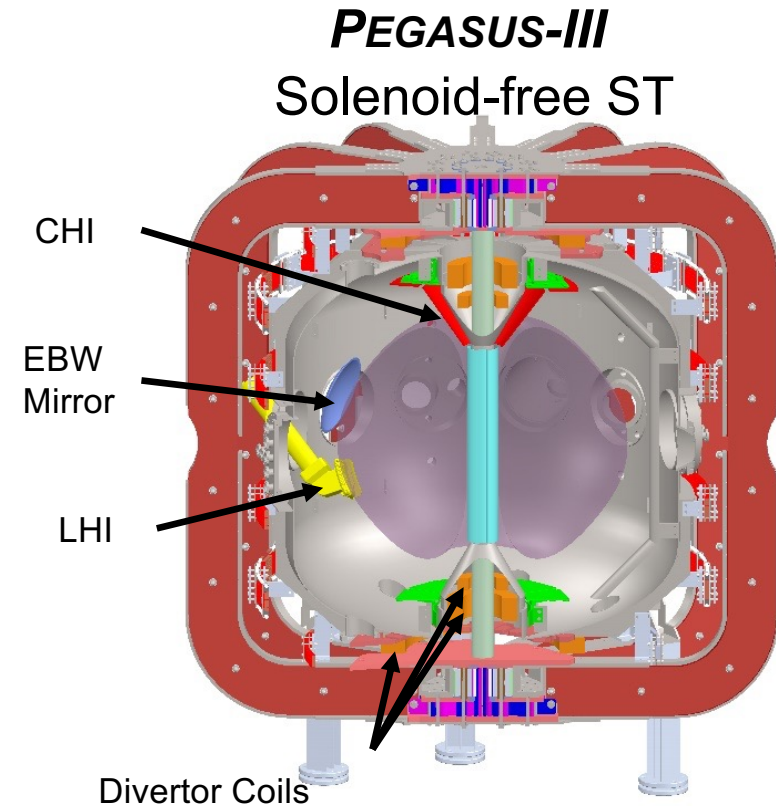


Measured microwave transmission in NSTX plasmas [%]



PEGASUS-III – lighting a match for fusion

- Future spherical tokamaks call for solenoid-free operation
 - Need to minimize solenoid due to shielding/cost
- Solenoid removal simplifies tokamak design
 - Potential cost reduction
 - More space for inboard shielding/blanket
 - Lower electromechanical stresses
- Major upgrade to Pegasus facility underway to compare/contrast/combine startup techniques
 - Local helicity injection
 - Coaxial helicity injection
 - EBW startup and sustainment
- University-class fusion facilities provide innovative approaches to fusion energy development



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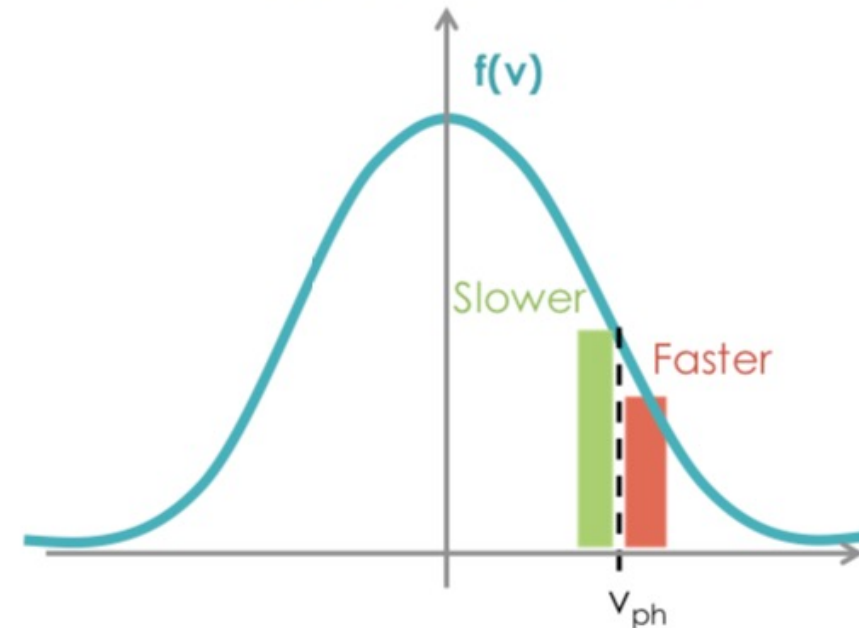
PEGASUS Website: Publications, Presentations
<http://pegasus.ep.wisc.edu>

Overview of plasma heating

- **Ohmic heating**
 - $P = V_{\text{loop}} * I_{\text{plasma}}$
 - Dissipative heating of current
 - Heats electrons
- **Neutral beam injection (NBI)**
 - Injection of high energetic neutral fuel atoms into plasma
 - Heating electrons and ions
- **Electron cyclotron resonance heating**
 - Inject microwaves with $\omega = \omega_{ce}$
 - Heats electrons
- **Lower hybrid resonance heating**
 - Inject waves with $\omega = (\omega_{ce}\omega_{ci})(1/2)$
 - Heats electrons and ions
- **Ion cyclotron resonance heating**
 - Injection of radio frequency waves with $\omega = \omega_{ci}$ (10s of MHz)
 - Heats ions
- **DC helicity injection**

Non-inductive current drive

- Particles with speed comparable to v_{ph} speed can resonate
- Particles with speed slightly slower than v_{ph} will be accelerated, take energy from wave
- Particles with speed slightly faster than v_{ph} will decelerate, give energy to wave
- This process alters the thermal distribution of particles and **results in a net current**
- Can also be achieved with tangential NBI

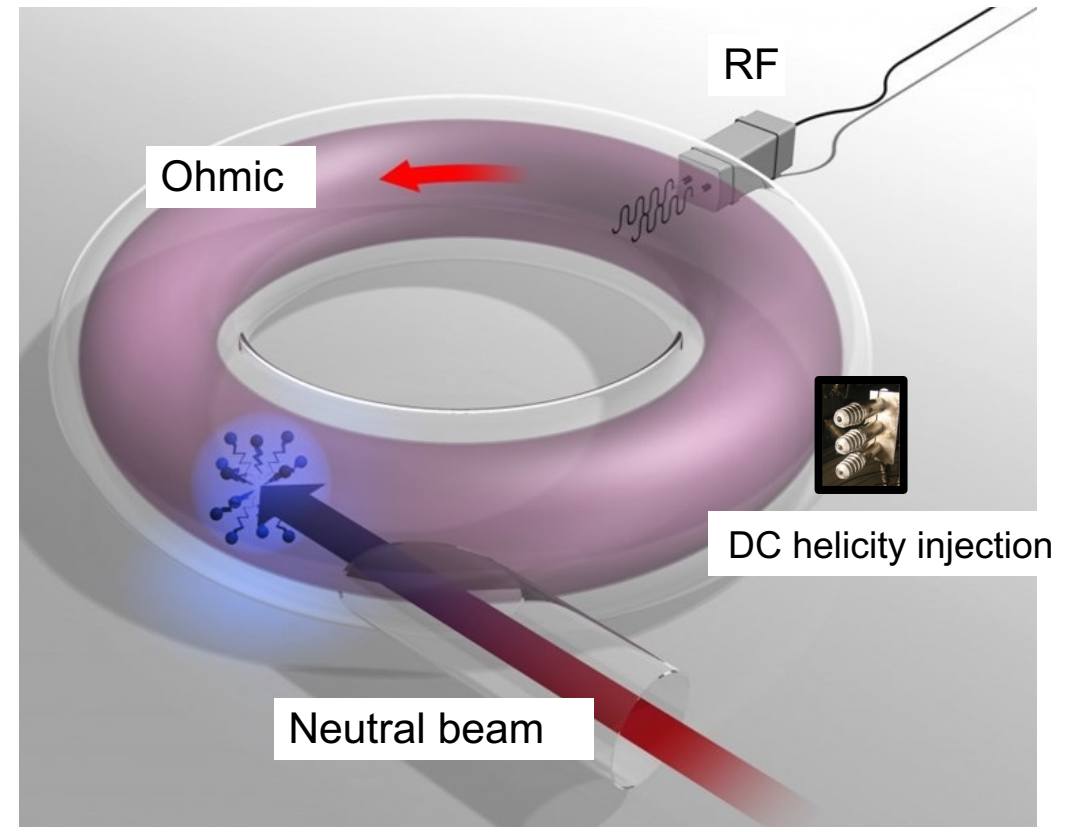


Tokamak plasmas require current drive and heating to achieve fusion

- Reaching ignition requires threshold for:

$$n \cdot T \cdot \tau_E$$

- External heating required to reach temperature for ignition
 - After ignition, self-heating sustains plasma
- Several methods of external heating & current drive available
 - Electron cyclotron (EC) resonance is in microwave range of frequencies
 - At high densities, injected microwave can be reflected – requires alternative methods of coupling microwave power
 - **DC helicity injection**



Why investigate startup for tokamaks?

- Compact toroidal geometry challenge for central solenoid
 - Also beneficial for ATs to minimize need for central solenoid
- Drives the search for non-solenoidal startup techniques
- Pegasus-III studies innovations in plasma startup techniques
 - Can we develop new startup methods to help reduce cost, complexity of future fusion power plants?
 - Are there any additional uses for this technology?

Pegasus-III Experiment

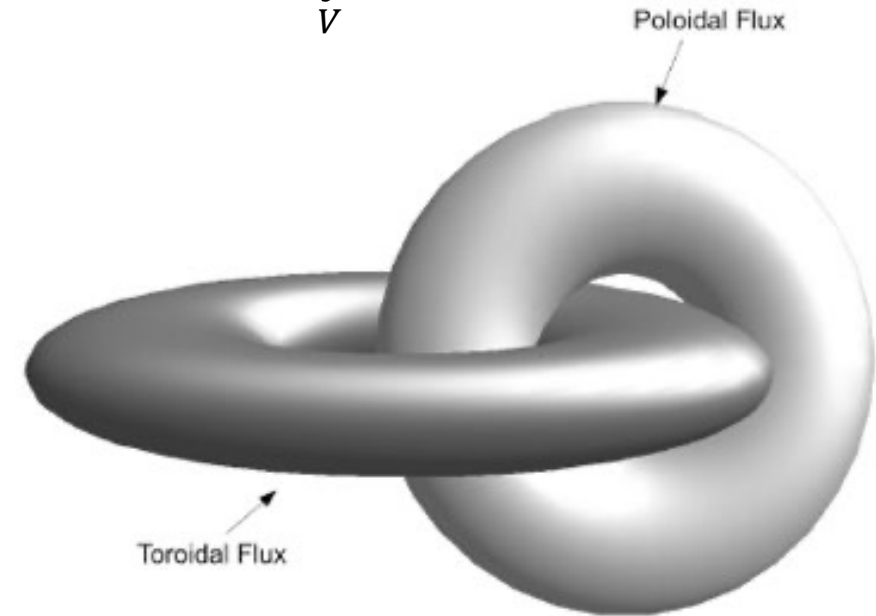


- New facility, 6.5 million Euros, for research in fusion energy and plasma science, UW-Madison
- Research team of 20+ people, funded at 2.5+ million Euros per year
- No ohmic solenoid!

Helicity injection techniques can initiate and drive tokamak plasmas


- Magnetic helicity, $K \equiv$ “linkedness” of magnetic flux
- In a tokamak, K_{plasma} results from linking toroidal and poloidal fluxes
 - Total $K \propto I_p \Phi$
 - Injecting $K \rightarrow$ increases I_p
- Two methods of adding helicity:
 - **AC helicity injection** – increasing flux via magnetic induction within target volume
 - **DC helicity injection** – potential applied along open field lines that penetrate magnetic boundary

$$K = \int_V \mathbf{B} \cdot \mathbf{A} dV$$



Schematic illustrating flux linkage in a toroidal (tokamak) geometry

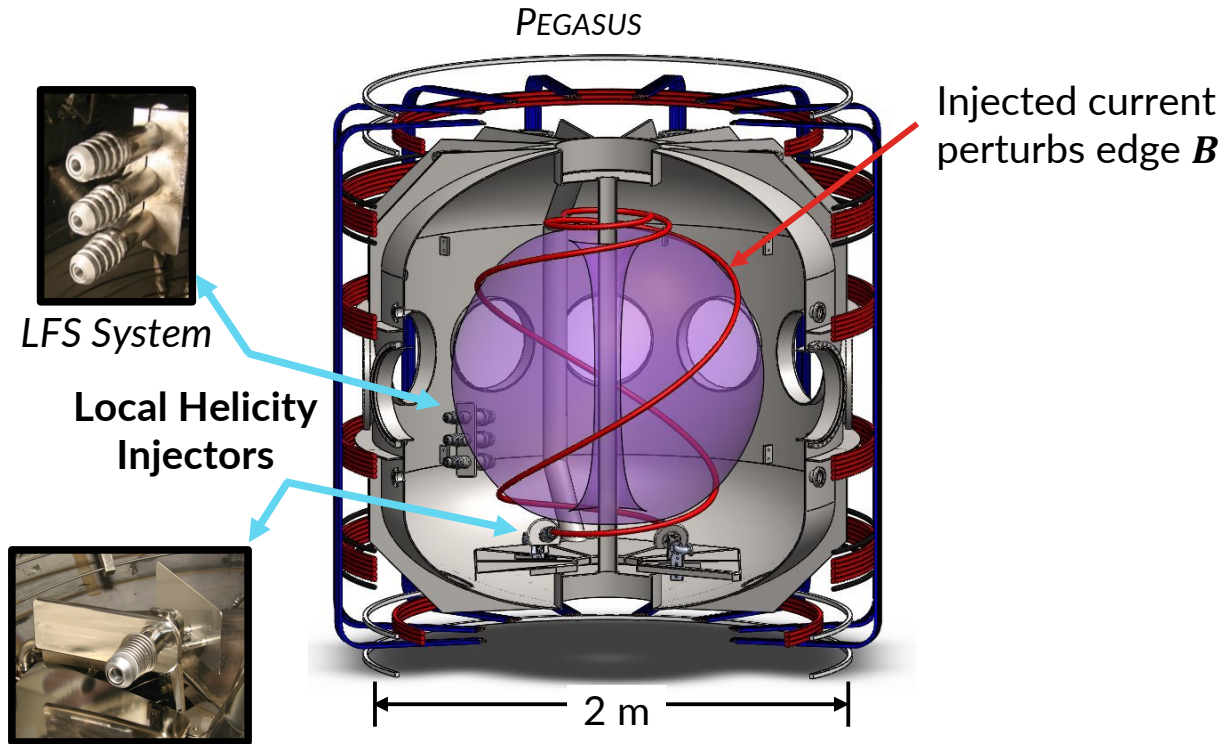
LHI Supplies Magnetic Helicity by Direct Current Injection

- Magnetic helicity K injected into the system¹: $K = \int \mathbf{A} \cdot \mathbf{B} dV$
- Helicity balance: $\frac{dK}{dt} = - 2\psi_T \frac{\partial \psi_p}{\partial t} - 2 \oint_S \phi \mathbf{B} \cdot \hat{n} dS - 2 \int_V \eta \mathbf{J} \cdot \mathbf{B} dV$


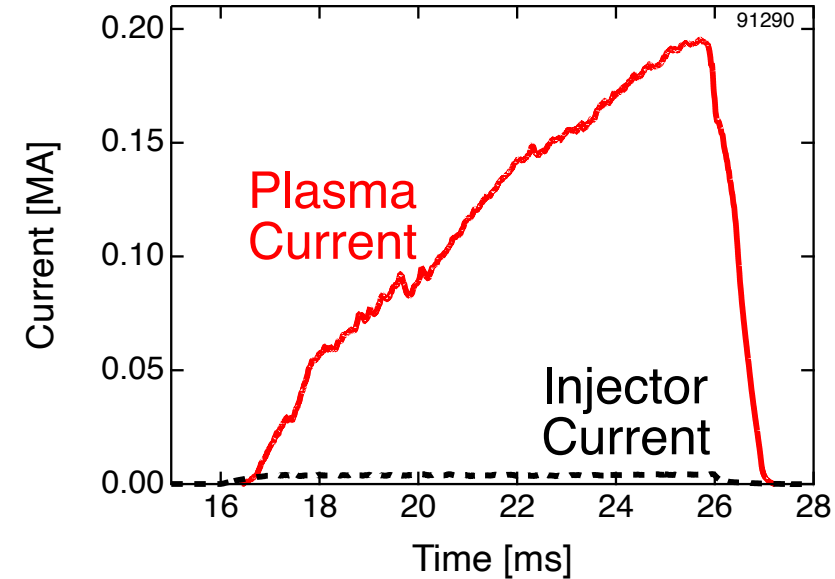
- Injecting current increases poloidal flux ψ_p linked with toroidal flux ψ_T from external coils
- Injection must be higher than dissipation for current drive

¹Berger, Plasma Phys. Control. Fusion **41** B167 (1999)

Local Helicity Injection (LHI) Provides Nonsolenoidal Startup



High Current Multiplication: $I_p \leq 0.2$
MA with $I_{inj} \leq 8$ kA



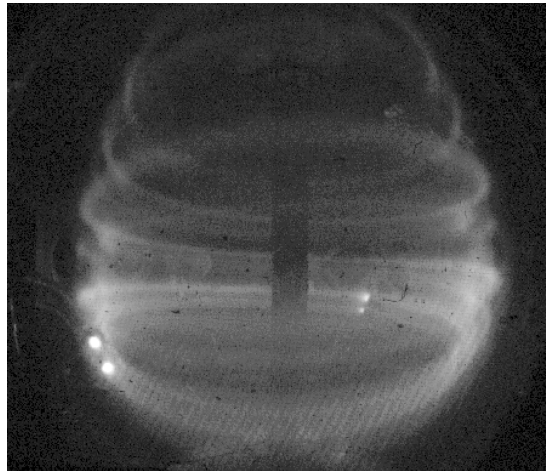
PEGASUS Parameters

A	1.15-1.3
R_0 [m]	0.2-0.45
a [m]	≤ 0.4
κ	1.4-3.7

- Edge current extracted from small, modular injectors
- Unstable current streams relax to tokamak-like state via helicity conserving instabilities

LHI Initiates a Tokamak-Like System

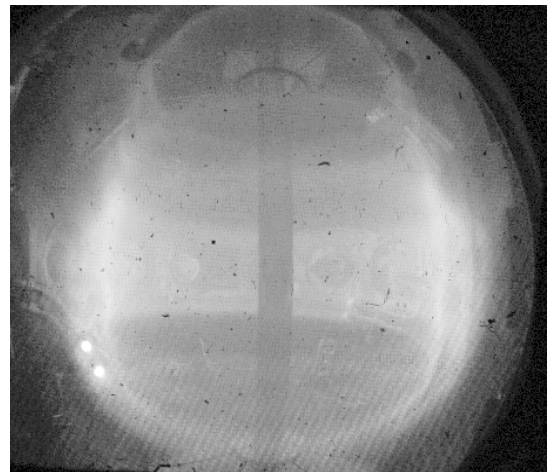
Fast Camera Images of LHI Stages



1. Injected current follows helical background field lines



$I_{inj} = 3-4$ kA per injector,
4 injectors total on Pegasus-III



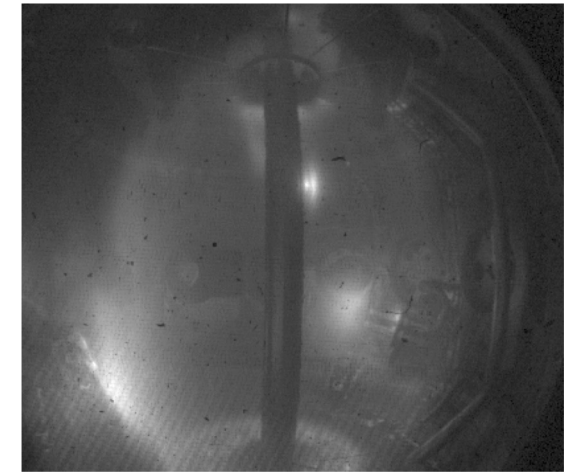
2. Current streams go unstable, reconnect



3. Plasma relaxes to a "tokamak-like" state



Majority of magnetic energy is in axisymmetric mode

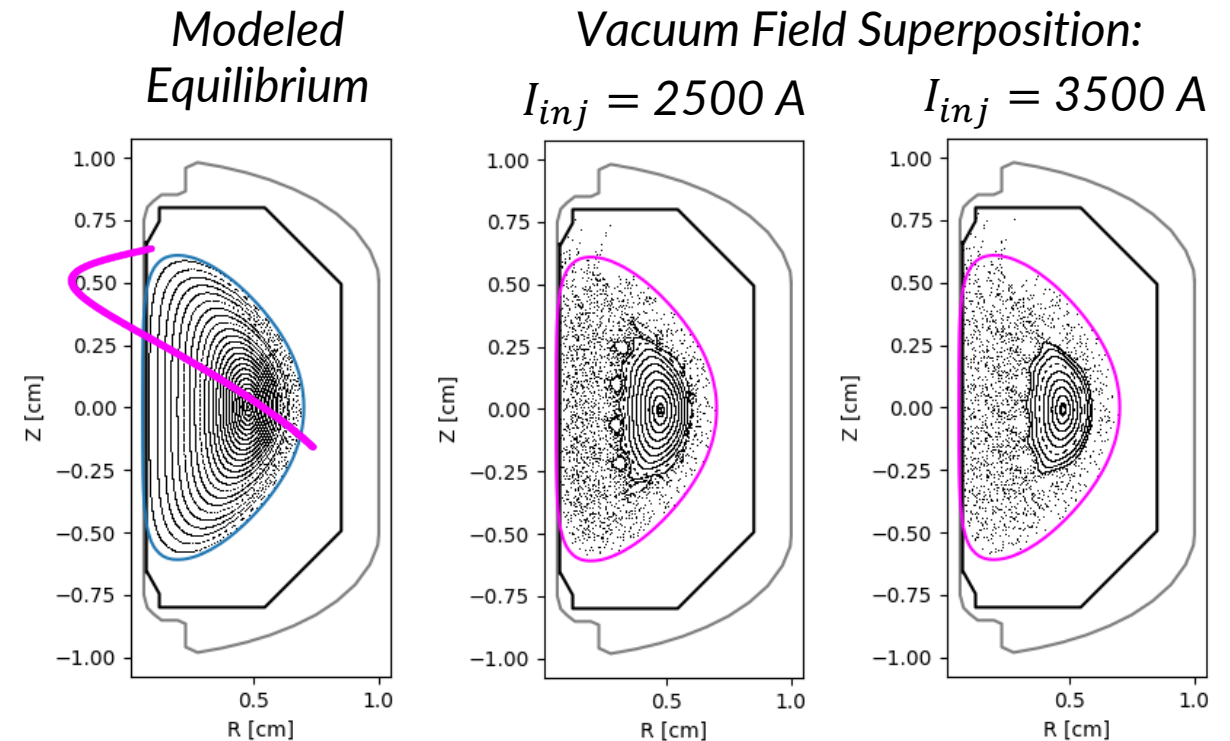


4. Tokamak plasma after injector shutoff: stream perturbation goes away

Perturbation Modeling Suggests Injected Current Stream Impacts Magnetic Topology

- Data consistent with 3D stream surrounding tokamak-like core
- FLARE: field line analysis and reconstruction environment
- Tool estimates impact of edge-localized stream on tokamak magnetic topology
- Vacuum approximation used for perturbation field
- Streams ergodize magnetic structure, potentially induce island structures

Implications for realized transport & confinement, scalability of LHI



not included yet

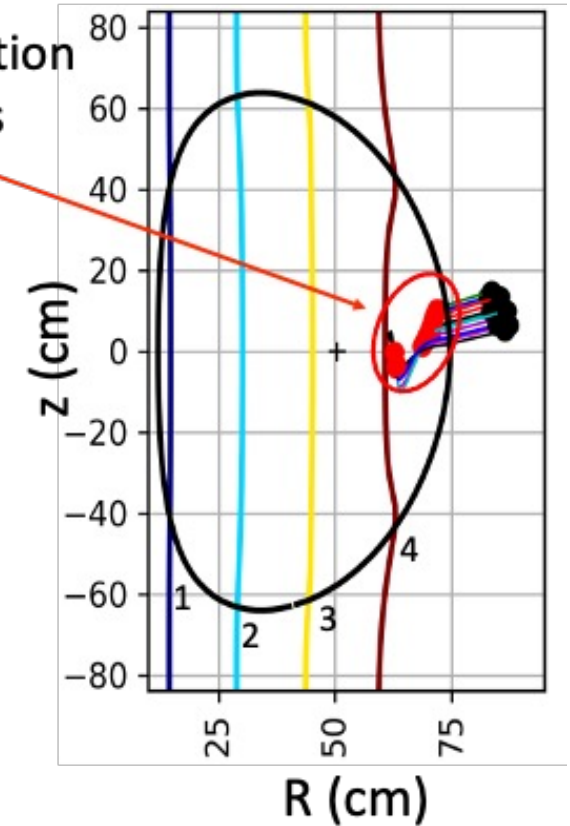
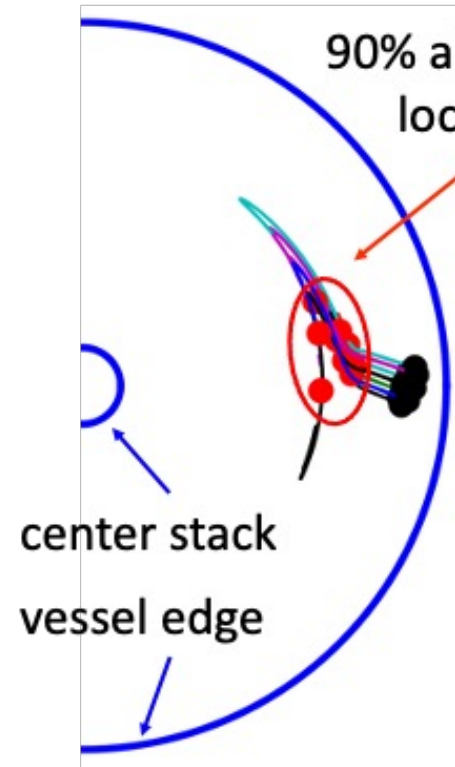
$$\mathbf{B}_{total} = \mathbf{B}_{equil} + \mathbf{B}_{pert, vacuum} + \mathbf{B}_{response}$$

Initial EBW program seeks to explore synergies

$B_T = 0.4 \text{ T}$

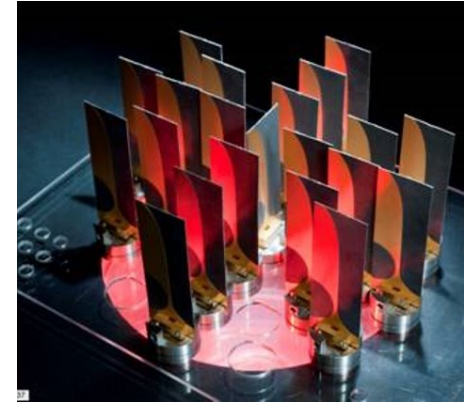
- Relative low B_T , high n_e of STs necessitates use of EBWs for fundamental absorption
- EBW heating: synergistically enhance LHI induced I_p current by lowering resistivity
 - 250 kW, 28 GHz
- T_e increases compatibility with non-inductive sustainment (i.e. neutral beam current drive)

Rays $x(t), y(t)$

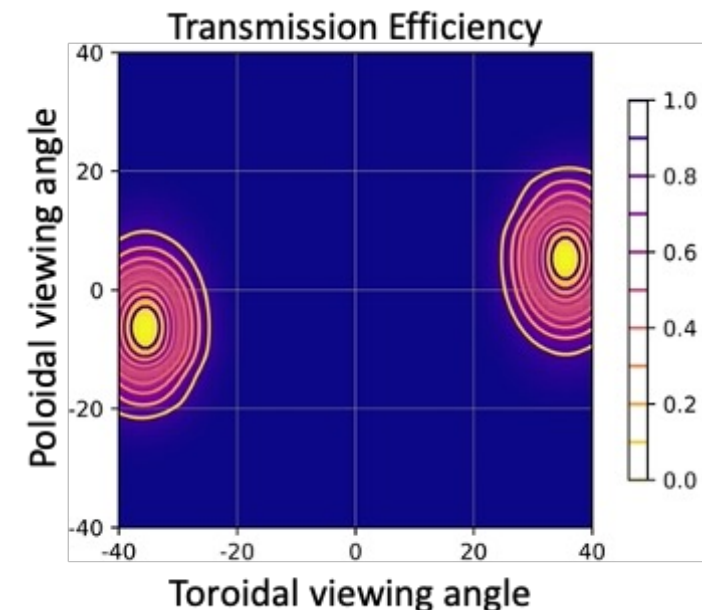


Future work will study impact of LHI streams on EBW mode conversion

- Insetable probes measure magnetic field fluctuations in plasma edge
 - $\dot{B}_z(R)$ and $\dot{\mathbf{B}}(R)$ array probes measure stream-related magnetic activity
 - Hall sensor probe measures equilibrium $\mathbf{B}(R)$
 - Significant magnetic fluctuations observed in Pegasus, $\frac{\delta B}{B_0} > 10^{-2}$
 - Post-HI heating will be pursued if large magnetic fluctuations prohibit coupling in plasma edge
- O-X mode conversion efficiency dependent on local magnetic field, density scale length
 - EBW emission measurements will be available in first run campaign
 - Thomson scattering will provide local n_e , T_e



Display of Vivaldi antennas used in SAMI diagnostic – collab with University of York



Plasma heating and current drive required for high performance fusion systems

- Burning plasma in fusion power plants will produce most of required heating power via alpha particles produced by fusion events
- Burning plasma will require auxiliary heating power:
 - initiate plasma
 - current ramp-up
- Plasma heating needed to reach ignition and provide
 - Control of MHD instabilities
 - Control against impurity events
 - Control plasma profiles
- Provide current drive for long-pulse or steady state operation

